

# Basis-set correction based on density-functional theory

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- 1 Slow basis-set convergence of wave-function theory
- 2 Basis-set correction based on DFT
- 3 Benchmarks and extensions

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- ▶ In the molecular electronic Hamiltonian

$$\hat{H} = \hat{T} + \hat{W}_{\text{ee}} + \hat{V}_{\text{ne}}$$

the **Coulomb electron-electron interaction**  $\hat{W}_{\text{ee}} = \sum_{i < j} 1/r_{ij}$  is singular as  $r_{ij} \rightarrow 0$ , leading to the **electron-electron cusp** (derivative discontinuity) in the eigenfunctions

$$\Psi(r_{ij}) = \Psi(0) \left[ 1 + \frac{1}{2} r_{ij} + \dots \right]$$

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- ▶ This leads to a **slow basis-set convergence of energies and many properties due to short-range correlation**

- ▶ The **full-configuration interaction (FCI)** ground-state energy in a basis set  $\mathcal{B}$  is

$$E_{\text{FCI}}^{\mathcal{B}} = \min_{\Psi \in \mathcal{W}^{\mathcal{B}}} \langle \Psi | \hat{T} + \hat{W}_{\text{ee}} + \hat{V}_{\text{ne}} | \Psi \rangle$$

where  $\mathcal{W}^{\mathcal{B}} = \{\Psi \in \mathcal{H}^{\mathcal{B}} \mid \langle \Psi | \Psi \rangle = 1\}$ .



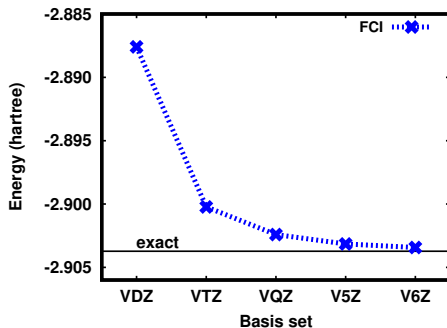
# Slow basis-set convergence of the FCI ground-state energy

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- ▶ Example of the He atom with the **series of basis sets**  $\mathcal{B} = \text{"cc-pVXZ"}$ :



- ▶ **Systematic but slow basis-set convergence**

## Two main strategies to deal with slow basis-set convergence

- ▶ **Extrapolation of the correlation energy to the CBS limit** using an inverse cubic law in  $X$ :

$$E_c^X = E_c^{\text{CBS}} + \frac{A}{X^3}$$

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- ▶ **Explicitly correlated R12/F12 methods** consisting in augmenting the two-electron Hilbert space by geminals of the form:

$$g_{i,j}(\mathbf{x}_1, \mathbf{x}_2) = \hat{Q}_{12} f(r_{12}) \hat{S}_{12} \phi_i(\mathbf{x}_1) \wedge \phi_j(\mathbf{x}_2)$$

where  $f(r_{12})$  is a correlation factor,  $\hat{S}_{12}$  is the rational generator ensuring the singlet and triplet cusp conditions, and  $\hat{Q}_{12}$  is the strong-orthogonality projector

Reviews: Ten-no, Noga, WIREs, 2012; Hättig, Klopper, Köhn, Tew, CR, 2012; Kong, Bischoff, Valeev, CR, 2012; Shiozaki, Werner, MP, 2013

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## Basis-set correction based on DFT (1/2)

- In **standard DFT** (complete basis set), the **exact ground-state energy** is expressed as

$$E_0 = \min_{\rho \in \mathcal{D}^{\text{CBS}}} \left\{ F[\rho] + \int v_{\text{ne}}(\mathbf{r})\rho(\mathbf{r})d\mathbf{r} \right\}$$

where  $\mathcal{D}^{\text{CBS}} = \{\rho \mid \exists \Psi \in \mathcal{W}^{\text{CBS}} \text{ s.t. } \rho_{\Psi} = \rho\}$  is the set of  $N$ -representable densities, and  $F[\rho]$  is the **Levy-Lieb universal density functional**

$$F[\rho] = \min_{\substack{\Psi \in \mathcal{W}^{\text{CBS}} \\ \Psi \rightarrow \rho}} \langle \Psi | \hat{T} + \hat{W}_{\text{ee}} | \Psi \rangle$$

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- ▶ **The restriction to densities representable in**  $\mathcal{B}$  **is much weaker than the restriction to wave functions representable in**  $\mathcal{B}$ , so we expect

$$E_{\text{FCI}}^{\mathcal{B}} \gg E_0^{\mathcal{B}} \gtrsim E_0$$

- ▶ We then **decompose the universal density functional**  $F[\rho]$  as

$$F[\rho] = \min_{\substack{\Psi \in \mathcal{W}^{\mathcal{B}} \\ \Psi \rightarrow \rho}} \langle \Psi | \hat{T} + \hat{W}_{\text{ee}} | \Psi \rangle + \bar{E}^{\mathcal{B}}[\rho]$$

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- ▶ We will consider a **non-self-consistent approximation** using the FCI wave function:

$$E_{\text{FCI+DFT}}^B = \langle \Psi_{\text{FCI}}^B | \hat{T} + \hat{W}_{ee} + \hat{V}_{ne} | \Psi_{\text{FCI}}^B \rangle + \bar{E}^B[\rho_{\Psi_{\text{FCI}}^B}]$$

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- ▶ We can also add the DFT basis-set correction to any **approximate wave-function theory (WFT) method**:

$$E_{\text{WFT+DFT}}^{\mathcal{B}} = E_{\text{WFT}}^{\mathcal{B}} + \bar{E}^{\mathcal{B}}[\rho_{\Psi_{\text{WFT}}^{\mathcal{B}}}]$$

# The complementary basis-set correction functional $\bar{E}^{\mathcal{B}}[\rho]$

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$$w_{ee}^{\mathcal{B}}(\mathbf{r}_1, \mathbf{r}_2)$$

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- ▶ **We fit this projected interaction by the long-range interaction used in range-separated DFT:**

$$w_{ee}^{\mathcal{B}}(\mathbf{r}_1, \mathbf{r}_2) \approx \frac{\text{erf}(\mu^{\mathcal{B}}(\mathbf{r}_1)r_{12})}{r_{12}}$$

with a local range-separation parameter  $\mu^{\mathcal{B}}(\mathbf{r})$ .

Giner, Pradines, Ferté, Assaraf, Savin, Toulouse, JCP, 2018

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$$\bar{E}_{\text{PBE}}^{\mathcal{B}}[\rho] = \int e_c^{\text{srPBE}}(\rho(\mathbf{r}), \nabla\rho(\mathbf{r}), \mu^{\mathcal{B}}(\mathbf{r})) \, d\mathbf{r}$$

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- ▶ **This approximate basis-set correction functional contains the physics of the electron-electron cusp, automatically adapts to each basis set  $\mathcal{B}$ , and correctly vanishes in the CBS limit**

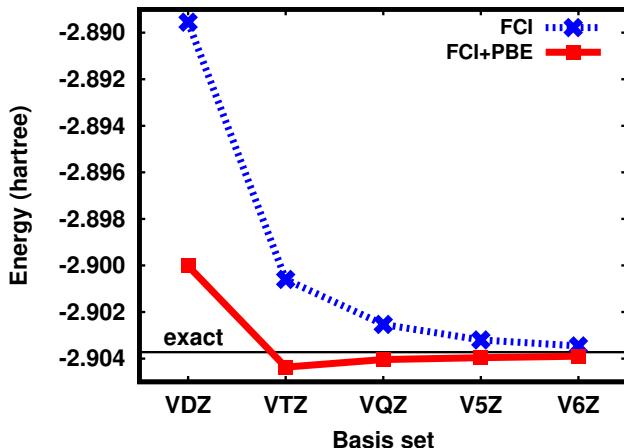
Giner, Pradines, Ferté, Assaraf, Savin, Toulouse, JCP, 2018

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# Convergence of the total energy with respect to the basis set

- ▶ Example of the He atom with the **series of basis sets**  $\mathcal{B} = \text{"cc-pVXZ"}$ :



- ▶ **Much faster basis-set convergence without altering the CBS limit**

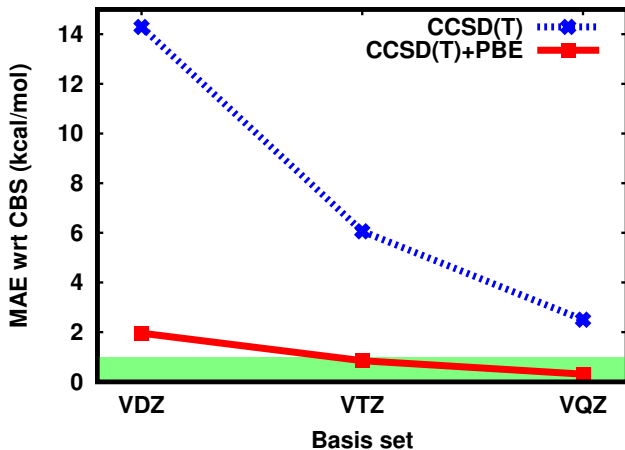
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# Benchmark on atomization energies of small molecules

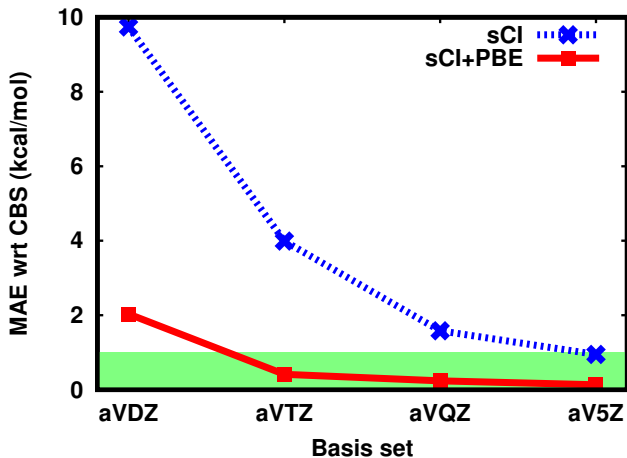
- ▶ Atomization energies of 55 small molecules (G2 set) with cc-pVXZ basis sets:



- ▶ MAE wrt CBS is below 1 kcal/mol already with the triple-zeta basis set

# Benchmark on dissociation energies of transition metal monoxides

- Dissociation energies of transition metal monoxides (ScO, TiO, VO, CrO, MnO, FeO, CuO) with selected CI calculations with aug-cc-pVXZ basis sets and pseudopotentials:



- MAE wrt CBS is below 1 kcal/mol already with the triple-zeta basis set

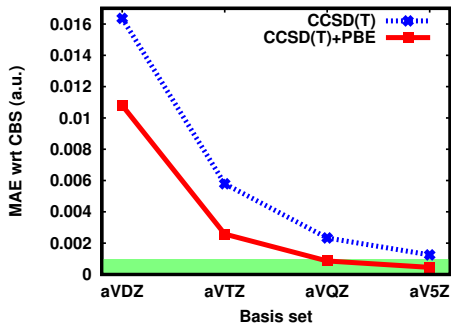
Yao, Giner, Anderson, Toulouse, Umrigar, JCP, 2021

# Benchmark on dipole moments of small molecules

- ▶ Calculation of the **dipole moment** by response to an electric field  $\mathcal{E}$ :

$$E_0^{\mathcal{B}}(\mathcal{E}) = E_{\text{WFT}}^{\mathcal{B}}(\mathcal{E}) + \bar{E}^{\mathcal{B}}[\rho_{\Psi_{\text{WFT}}^{\mathcal{B}}}(\mathcal{E})] \implies d_0^{\mathcal{B}} = - \left. \frac{dE_0^{\mathcal{B}}(\mathcal{E})}{d\mathcal{E}} \right|_{\mathcal{E}=0}$$

- ▶ **Dipole moments of 14 small molecules** with aug-cc-pVXZ basis sets:

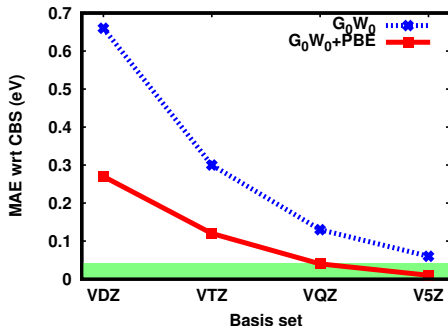


- ▶ The basis-set correction also accelerates the convergence of dipole moments, albeit to a lesser extent

- ▶ Extension to many-body Green-function theory for GW calculations:

$$E_0^{\mathcal{B}} = \text{stat}_{G^{\mathcal{B}}} \left\{ \Omega^{\mathcal{B}} [G^{\mathcal{B}}] + \bar{E}^{\mathcal{B}} [\rho_{G^{\mathcal{B}}}] \right\} \implies (G^{\mathcal{B}})^{-1} = (G_0^{\mathcal{B}})^{-1} - \Sigma_{\text{Hxc}}^{\mathcal{B}} [G^{\mathcal{B}}] - \bar{V}^{\mathcal{B}} [\rho_{G^{\mathcal{B}}}]$$

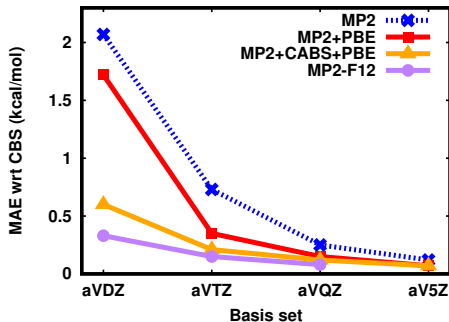
- ▶ IPs of 20 small molecules by the  $G_0W_0$  method with cc-pVXZ basis sets:



- ▶ The basis-set correction also accelerates the convergence of  $G_0W_0$

# Density-fitting implementation and benchmark on reaction energies

- ▶ Implementation in MOLPRO with **density-fitting calculation of the local range-separation parameter**  $\mu^B(\mathbf{r})$  with scaling  $O(N_{\text{occ}} N_{\text{basis}} N_{\text{fit}} N_{\text{grid}})$
- ▶ **51 reaction energies** (FH51 set) with aug-cc-pV(X+d)Z basis sets:



- ▶ The CABS single-excitation correction is important for small basis sets
- ▶ MP2-F12 is more accurate, especially for the double-zeta basis set

Heßelmann, Werner, Knowles, Giner, Reinhardt, Toulouse, work in progress

## ► Summary:

- DFT basis-set correction which automatically adapts to each basis set
- based on pre-existing short-range correlation functional
- accelerates basis-set convergence of energies and properties
- implemented in **QUANTUM PACKAGE** and **MOLPRO**

## ► Outlook:

- Construction of a more rigorous basis-set correction functional
- Extension to linear-response theory

## ► Contributors to this work:

**Paris:** R. Assaraf, A. Ferté, **E. Giner**, B. Pradines, P. Reinhardt, A. Savin, D. Traore

**Toulouse:** P.-F. Loos, A. Scemama

**Cornell:** Y. Yao, T. Anderson, C. Umrigar

**Molpro team:** A. Heßelmann, P. Knowles, H.-J. Werner