

# Multiscale Modelling of Gold Clusters and Nanoparticles

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# Outline

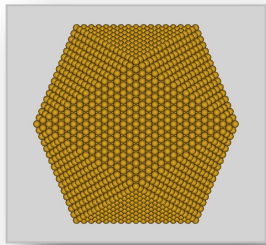
1. Introduction & motivation
2. Simulation method
3. Thiol adsorption simulations
4. Nanocrystals in superlattices
5. DFT calculations of gold nanoclusters
6. Conclusions
7. The future

# Introduction

## Our object of interest

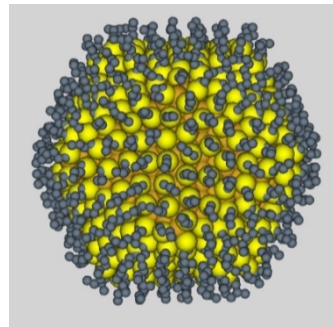
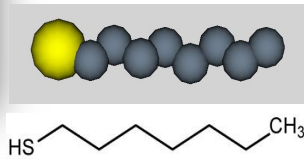
From the bottom to the top

NANOCRYSTAL  
OF GOLD

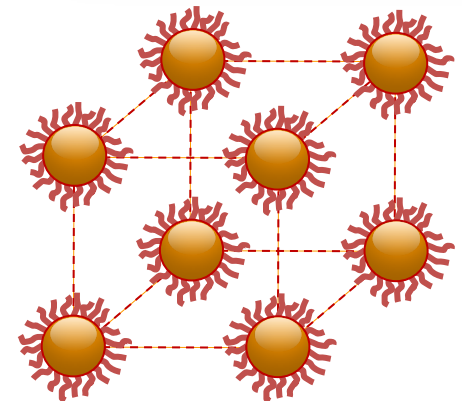
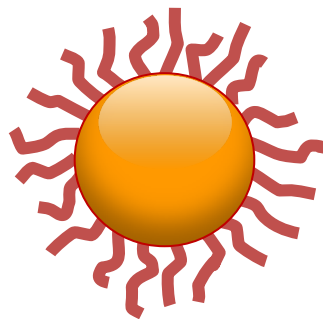
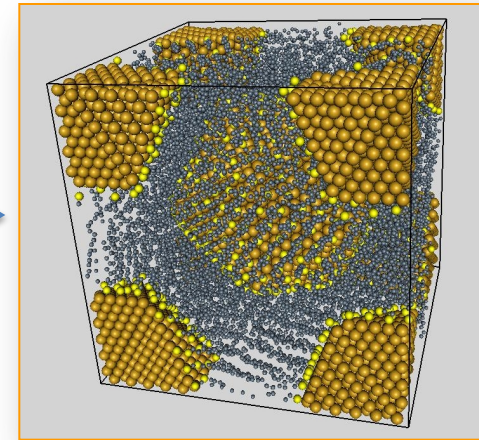


Icosahedron

Adsorption  
of thiols



Formation of  
superlattices



# 1. Introduction

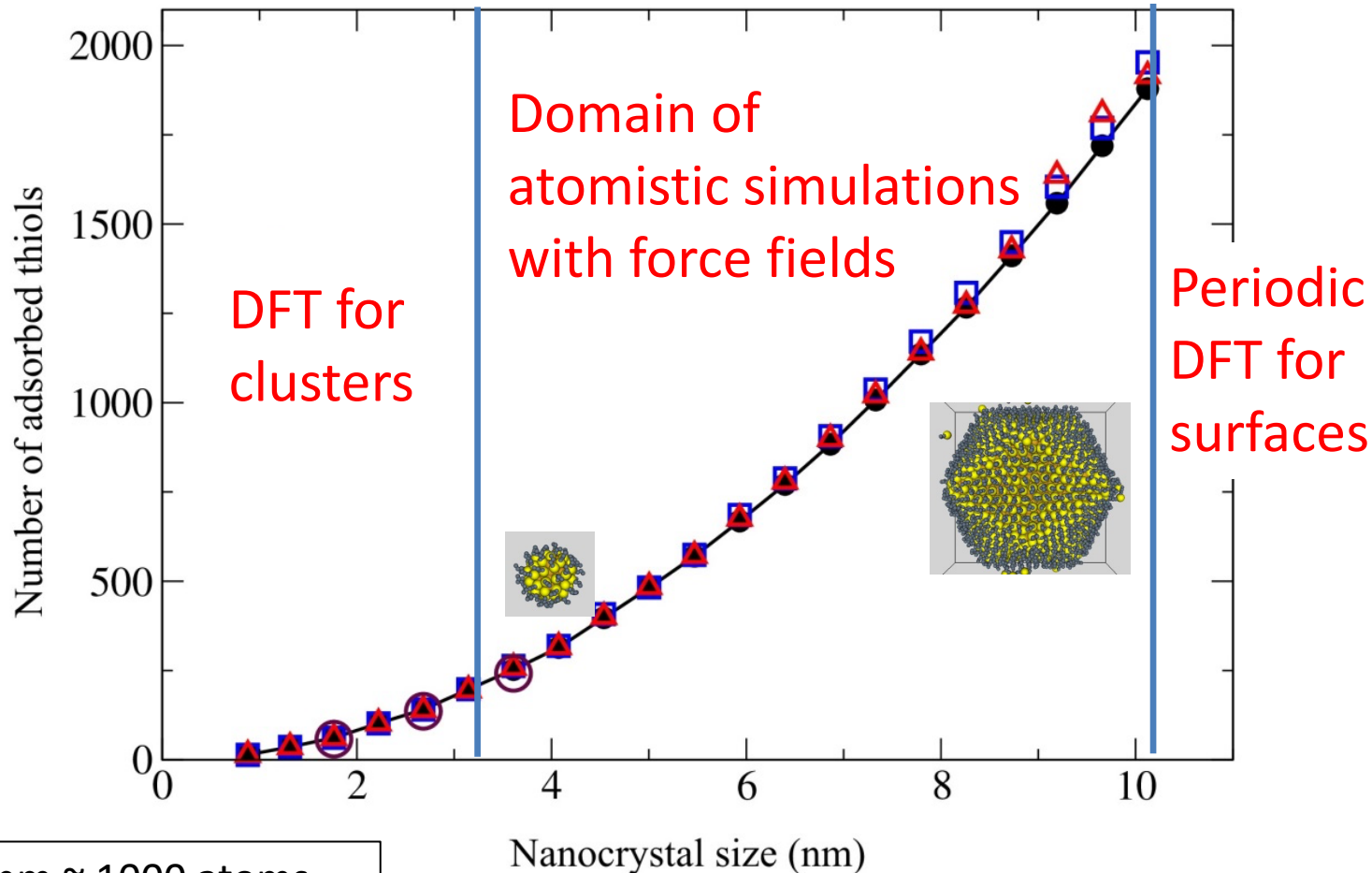
## Unsolved problems in nanoparticles science:

1. What does **control the growth** of nanoparticles?
2. How do **ligands adsorb** on nanoparticles?
3. How do **nanoparticles interact**?
4. How can we **control the assembly** of nanoparticles?
5. How do some nanoparticles **catalyze reactions**?
6. How nanoparticles can be **used in applications**?



## 2. Simulation method

Why do we use classical methods?



2 nm ~ 1000 atoms  
5 nm ~ 10000 atoms  
10 nm ~ 50000 atoms

Nanocrystal size (nm)

Nanocrystals between 3 and 10 nm cannot be studied by quantum chemical methods.

## 2. Simulation method

### Natomos-Gromacs: acceleration of simulations

- Simulations limited to nanocrystal diameter of 5 nm in literature.
- Nanocrystals between 4 and 10 nm in many experiments.
- **Our simulations: nanocrystals until 10 nm never reached before.**

### Simulation methods

#### Natomos

Home-made Monte Carlo &  
Molecular Dynamics code



#### Gromacs

Public Molecular Dynamics code  
**massive parallel computing**

#### NATOMOS



#### GROMACS



#### NATOMOS



- Definition of configuration
- Parameterization of force field

MD simulations

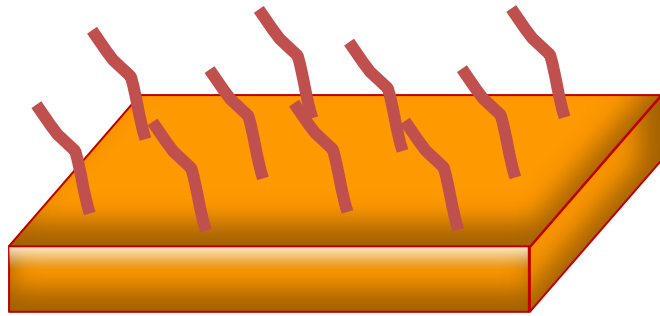
Analysis of results

**Up to 400x faster simulations**

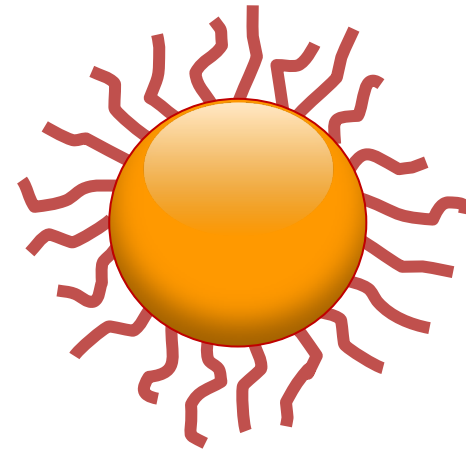
### 3. Thiols adsorption simulations

How do **ligands adsorb** on nanoparticles?

Why can we put more ligands on a nanocrystal surface ?



Au(111) planar surface<sup>1</sup>  
21.4 Å<sup>2</sup>/thiol

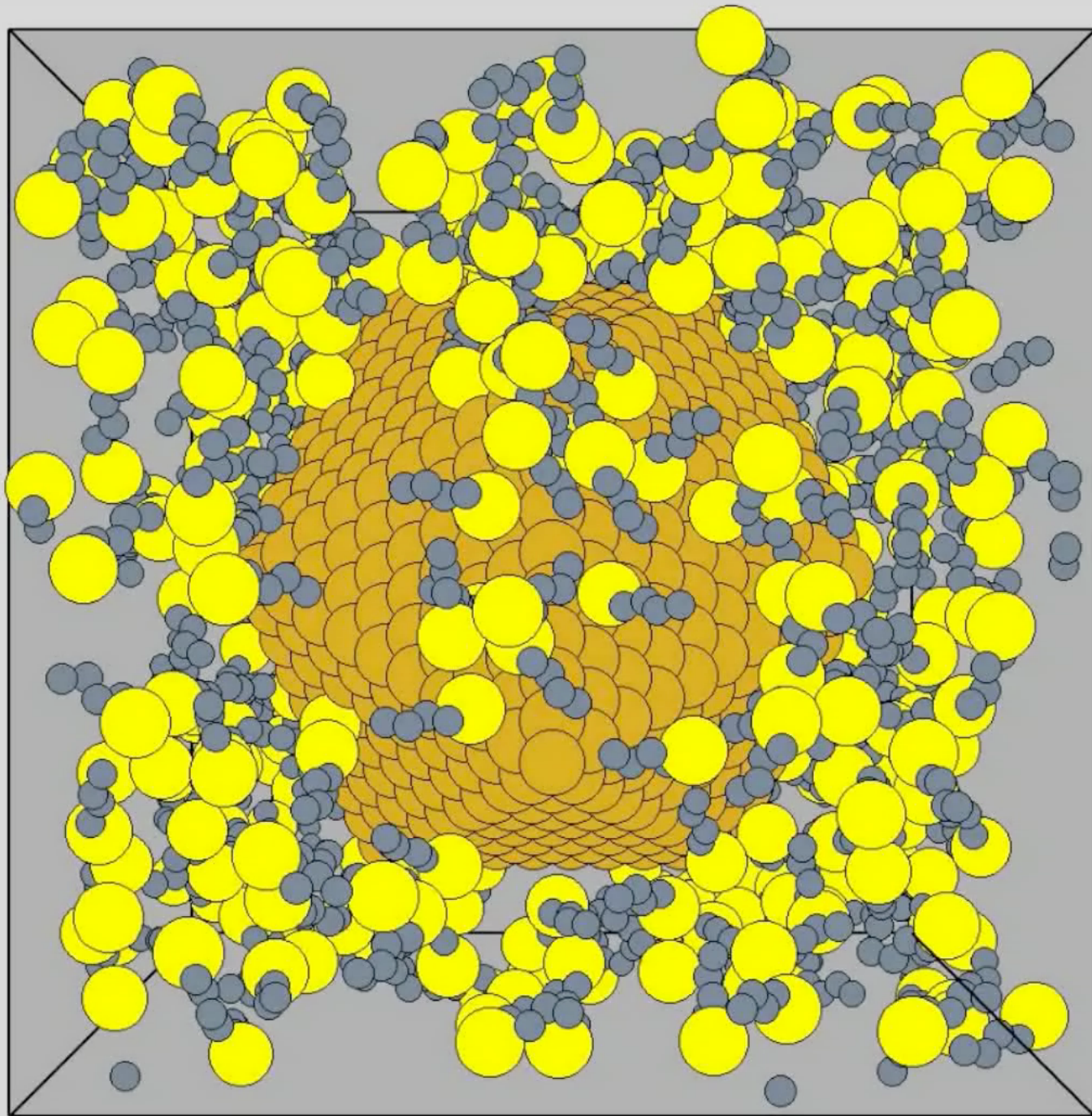


Au nanocrystal<sup>2</sup>  
15.2 - 17.2 Å<sup>2</sup>/thiol

From which size does a nanocrystal behaves like the bulk material?

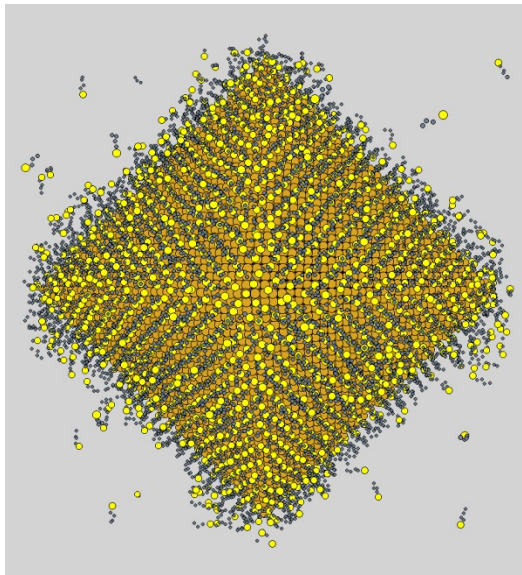
1: Ulman. Chemical Reviews 1996. 96. 1533–1554.

2: Lennox *et al.* Chemistry – A European Journal 1996. 2. 359–363.



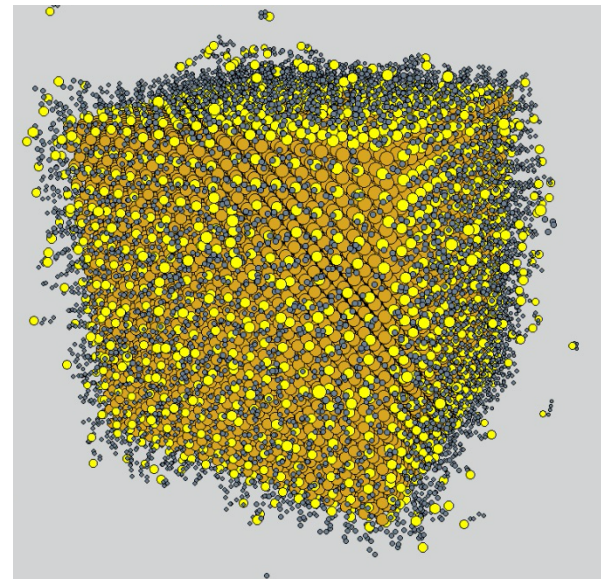


# Octahedron vs Cube



octahedron

versus

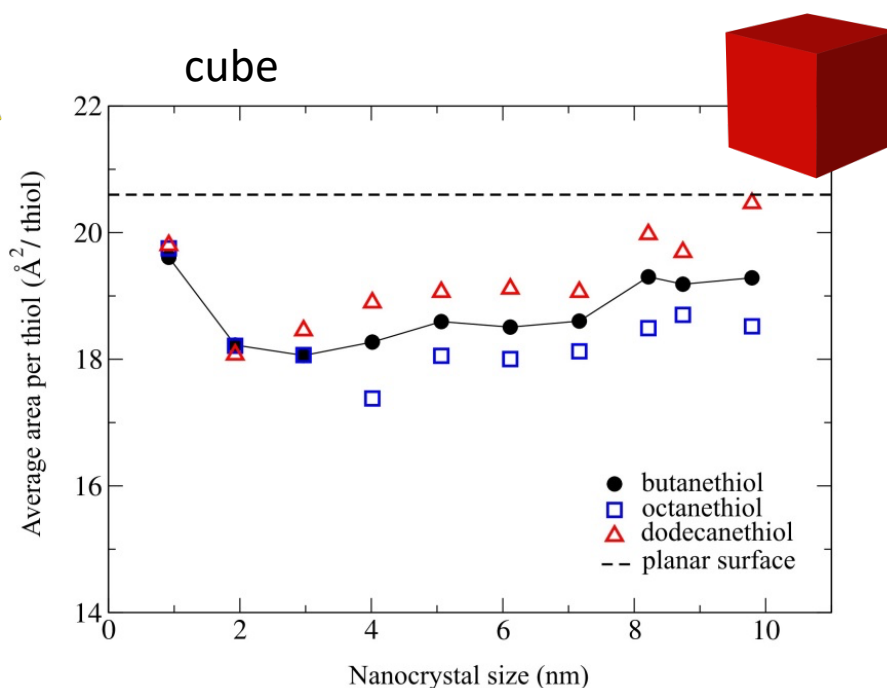
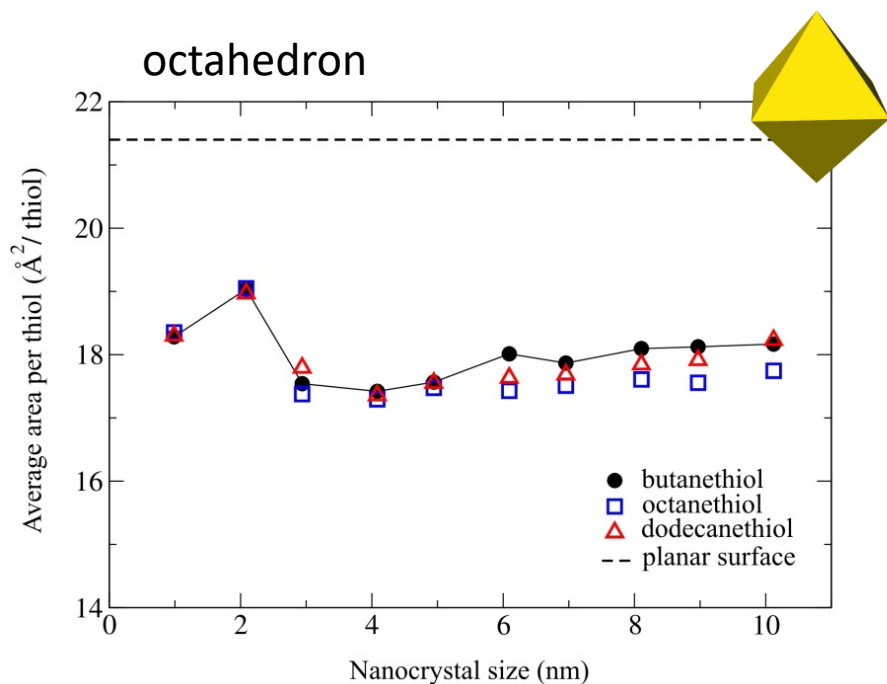


cube

1. T. Djebaili, J. Richardi\*, A. Abel et M. Marchi, J. Phys. Chem. C 117, 17791 (2013)
2. T. Djebaili, J. Richardi\*, A. Abel et M. Marchi, J. Phys. Chem. C 119, 21146 (2015)

### 3. Thiols adsorption simulations

## Average area per thiol



- **Good agreement with experimental data** by mass spectroscopy<sup>1</sup>, thermogravimetry<sup>2</sup> and TEM,
- Small difference between cube and octahedron,
- The surface coverage slightly depends on the thiol chain length.

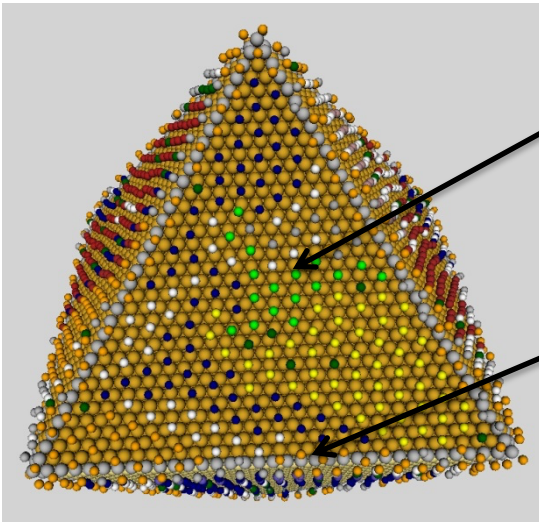
1. Lämmerhofer *et al.* ACS Nano 2013. 7. 1129–1136

2. Hostetler *et al.* Langmuir 1998, 14, 17–30.

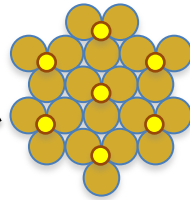
## Thiol headgroup organization

What is the origin of the lower area per thiol? – It's the edges, stupid!

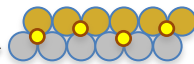
Octahedron (111) facets



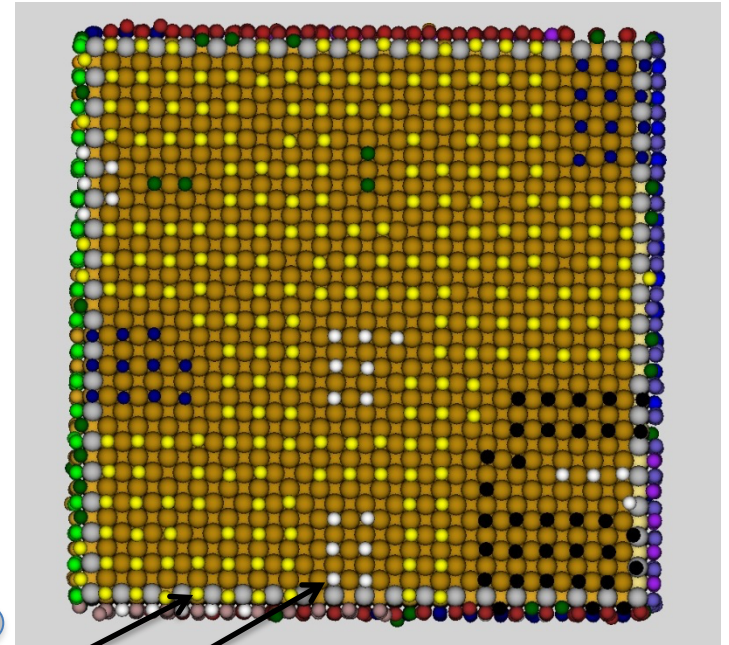
Hexagonal SAM



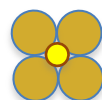
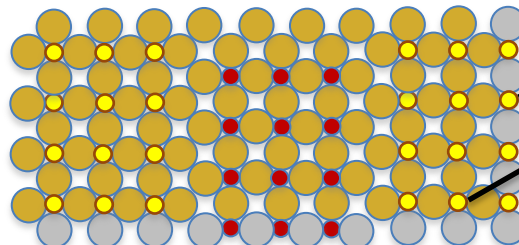
Zigzag SAM



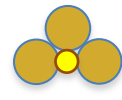
Cube (100) facets



Square SAM



4f- hollow



edge sites

- Two different molecular organizations on the facet center & edges.

- occupation of new sites on the edges



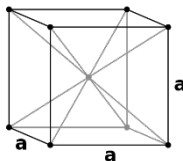
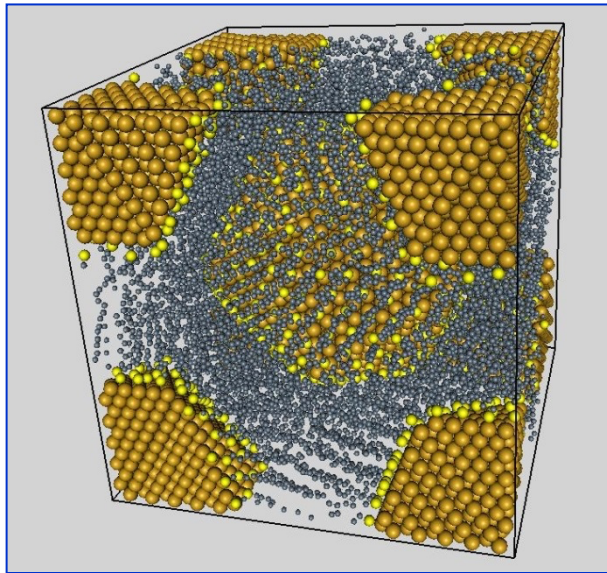
## 4. Nanocrystals in superlattices

### How do nanoparticles interact?

#### Simulation of BCC and FCC superlattices

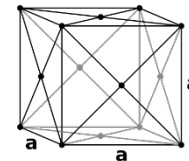
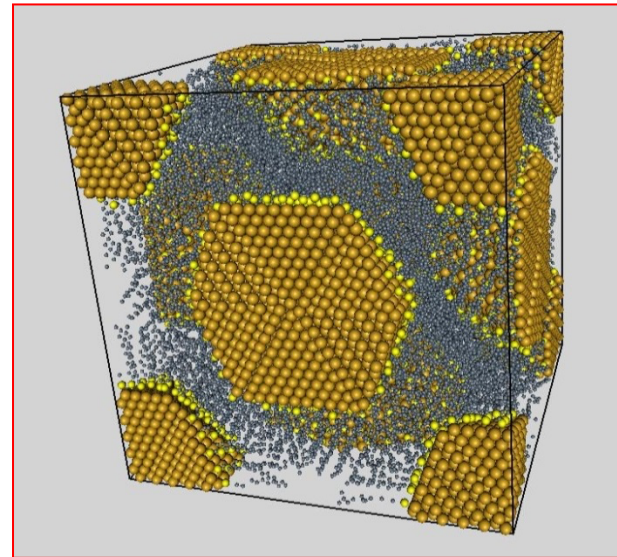
BCC

Body Centered Cubic



FCC

Face Centered Cubic

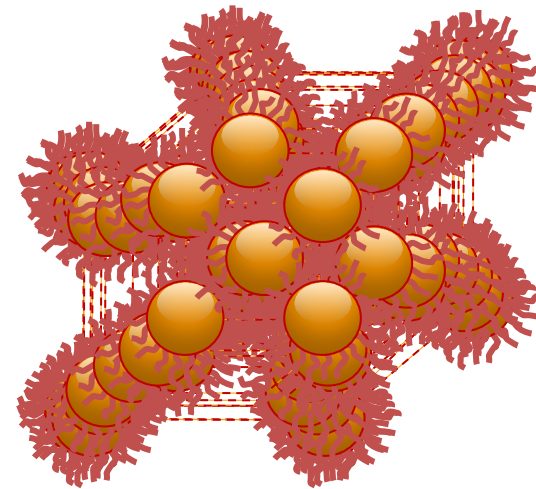
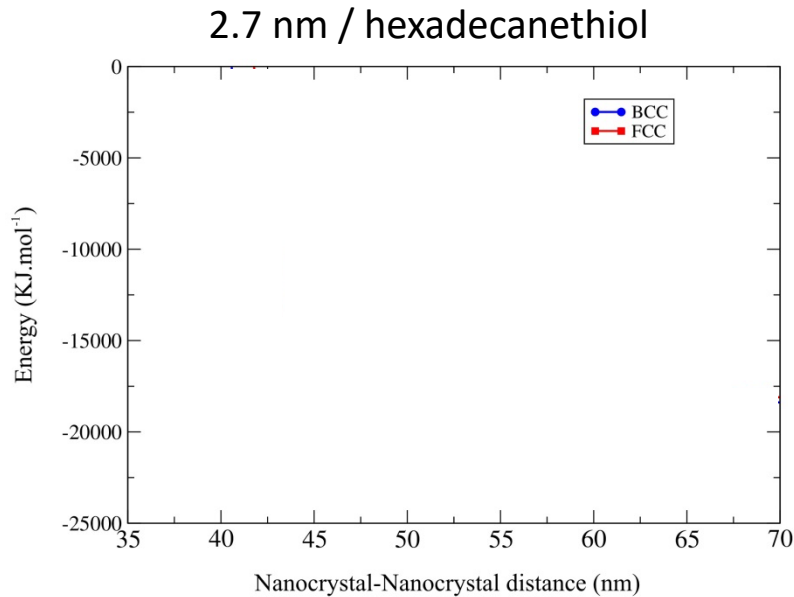




## 4. Nanocrystals in superlattices

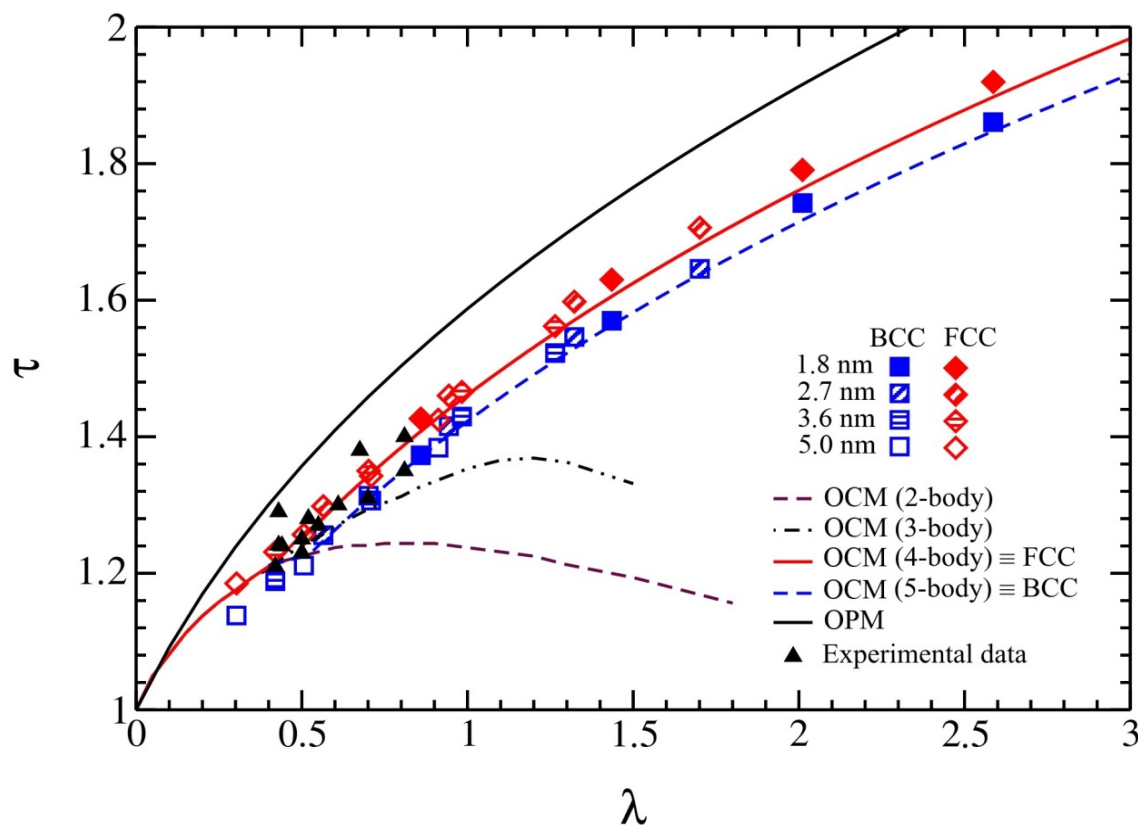
Method : evolution of potential energy with Nanocrystal-Nanocrystal distance

- Simulation results :
- Lattice type: structure with the lowest energy.
  - Optimal Nanocrystal-Nanocrystal distance.



Smaller nanocrystal distance in BCC

## Evolution of the nanocrystal distance with ligand length



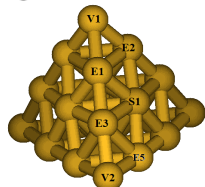
NC-NC distance  
measurement  
error :  $\pm 0.2\%$

- **Excellent agreement with OCM theory.** OPM theory by Landman is wrong.
- This shows the importance of **many-body interactions**.
- The smaller Nanocrystal-Nanocrystal distance in BCC can be confirmed.

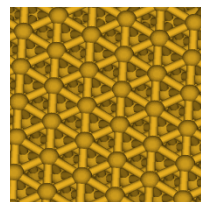
# Methods for gold clusters and periodic surfaces

## Ab initio calculations

Software: Quantum espresso  
DFT: PBE (GGA functional)  
Pseudopotentials: Ultrasoft



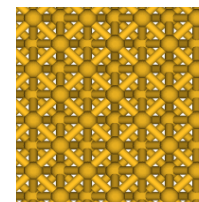
Au<sub>20</sub> Pyramid



Au(111)



Optimized geometries  
Relative energies



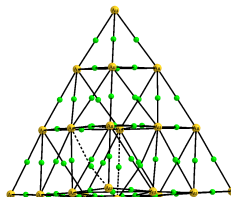
Au(100)

## Quantum theory of an atom in molecule (QTAIM)

Generation of density file:

Gaussian09,  
PBE/mod-LANL2DZ<sup>1</sup>

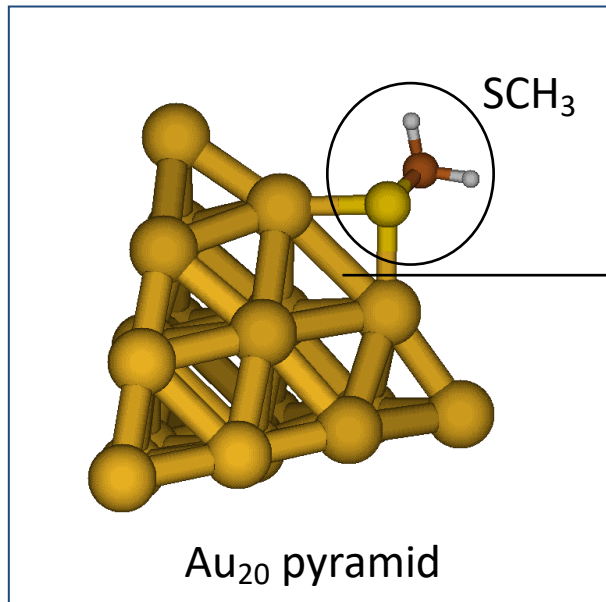
Topological Analysis  
AIMStudio



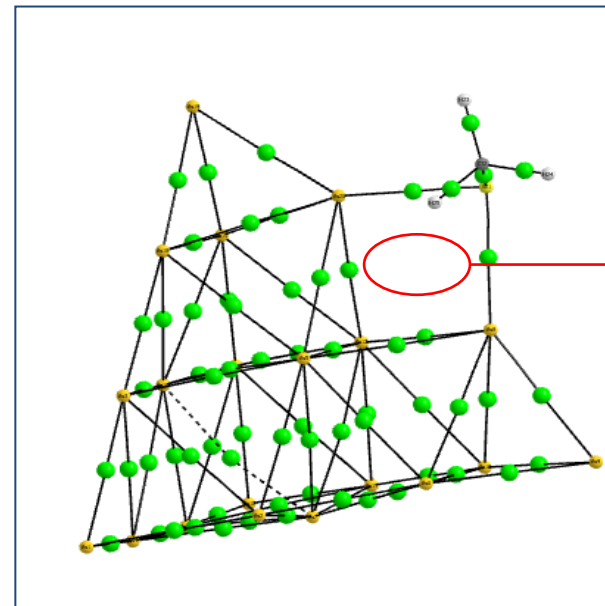
Critical points analysis  
(Bond, ring, cage)  
Partial charges per atom

**Energy, geometry and physical criteria for bond breaking**

## Example: Au<sub>20</sub>-Methyl thiolate



Most stable isomer

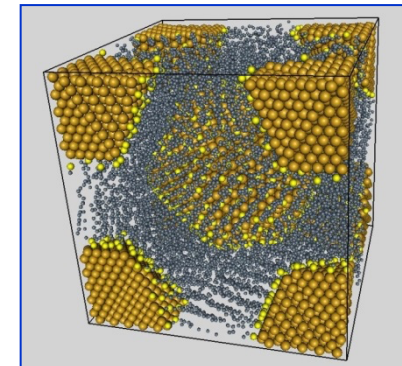
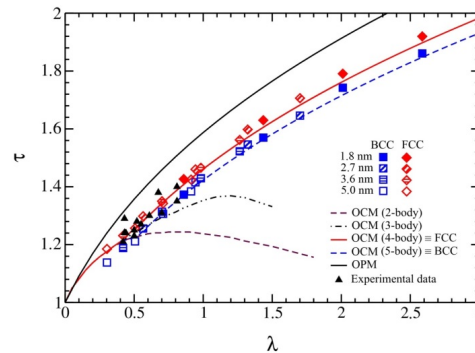
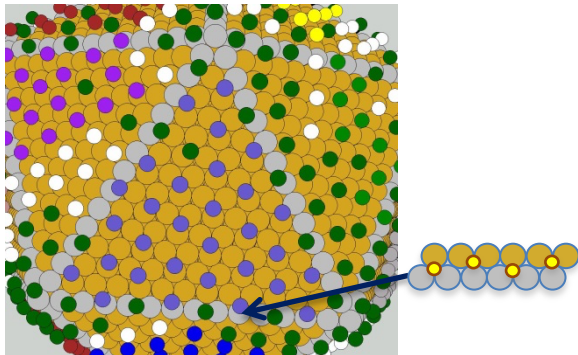


Green: bond critical points

**For larger Nanocrystals:  
Use these informations to improve Reax force fields  
for diffusion of gold atoms and Au-Au / Au-S bond breaking**

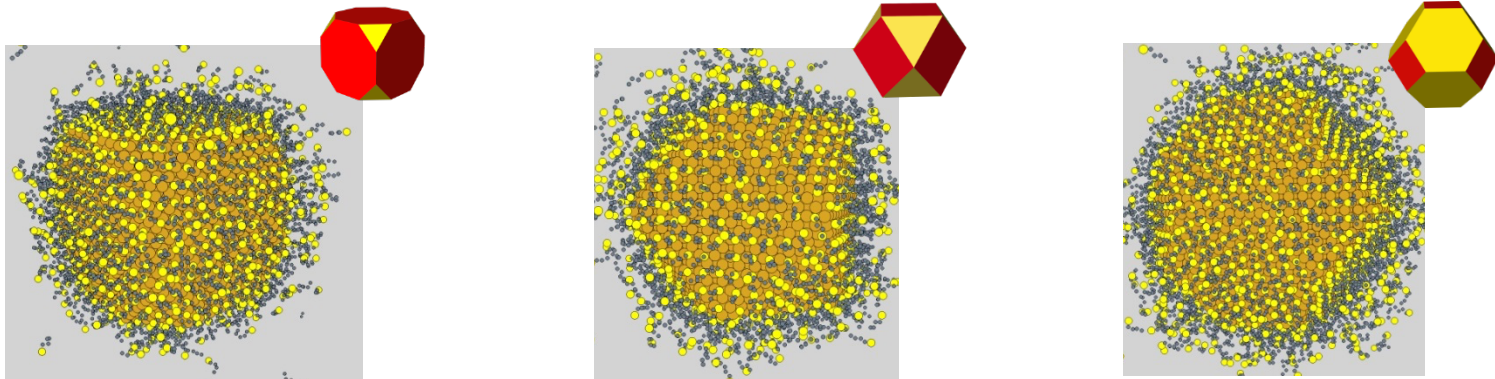
## 5. Conclusions

- How do **ligands adsorb** on nanoparticles?
- We reproduce experimental surface coverage.
- Edges are the origin of different surface coverage for nanocrystals..
- A new molecular organization on the edges.
- Bond breaking due to thiolate adsorption
- How do **nanoparticles interact**?
- We reproduce experimental distances.
- Distances are related to **many body interactions**.



# Perspectives

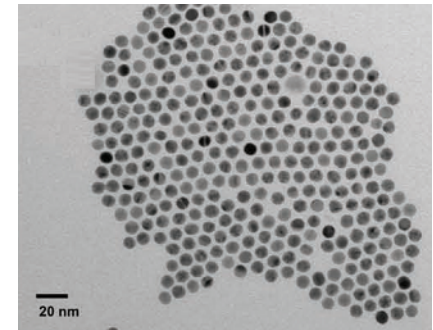
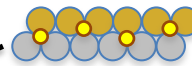
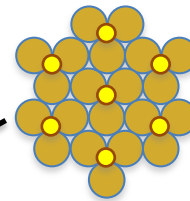
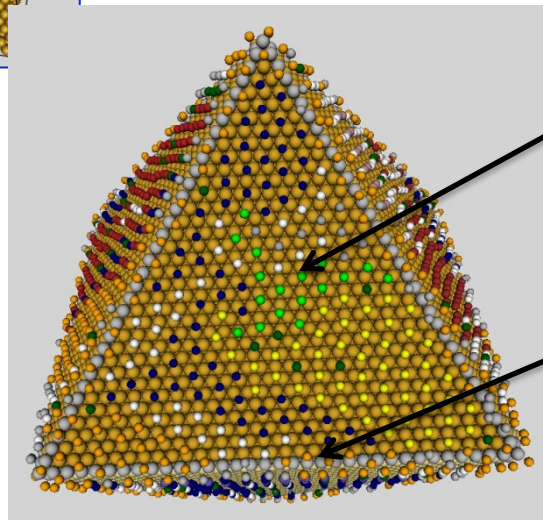
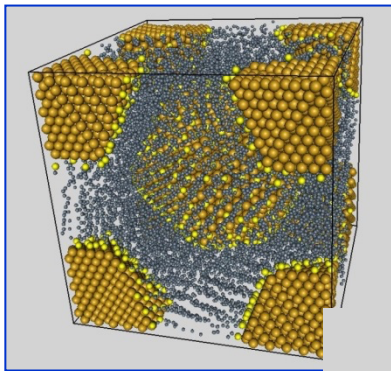
- Improve force fields.
- New materials (Ag, Pt, Co, Cu).
- Addition of solvent (e.g: hexane).
- Simulation of non ideal truncated NCs shapes.



- Analysis of dynamic & structural properties of ligands :
  - ligand diffusion.
  - tilt angle.
  - frequency of trans conformations.

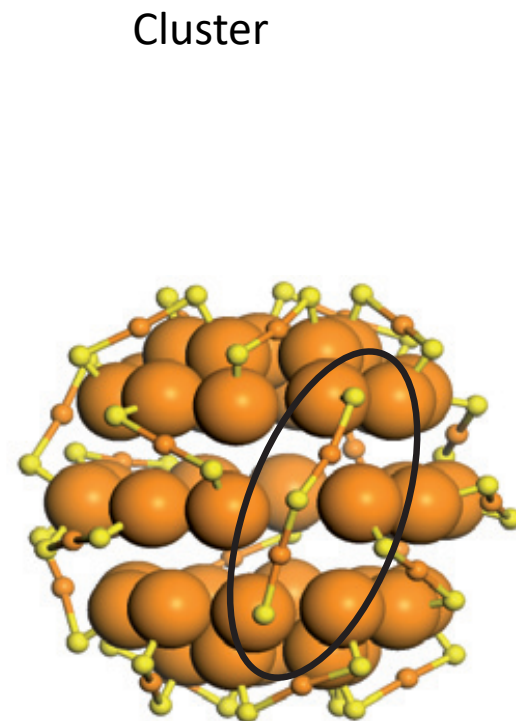
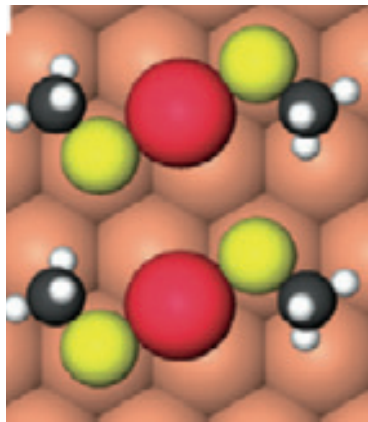
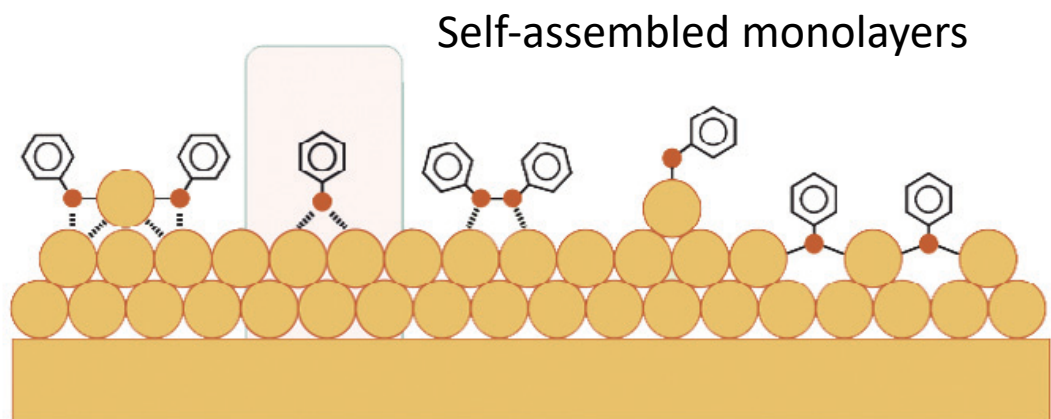


# THANK YOU



# Perspectives

*A revolutionary finding : S – Au – S lines on gold.*



1. Häkkinen, H. Nature Chemistry, 2012, 4, 443-455.
2. Jadzinsky et al. Science 2007 318, 430-433.
3. Cossaro, A. et al. Science 2008 321, 943-946.



# Perspectives

Current interaction models do not give these S-AU-S lines.



We need better interaction models including polarizability:

- Polarization  $> 20\%$  of binding energies for molecules on gold.
- important charge transfer of  $-0.33 e$  between silver and thiolates

Li, A.; Piquemal, J. P.; Richardi, J.; Calatayud, M. Butanethiol adsorption and dissociation on Ag (111): A periodic DFT study. Surf. Sci., 2016, 646, 247-252

## Interaction model

## Intramolecular interaction parameters

$$U_{intra} = U_{bond} + U_{bend} + U_{torsion}$$

(Dubbeldam *et al.* JPC. B 2004)

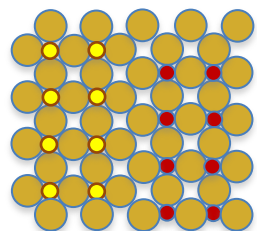
## Intermolecular interaction parameters

$$U_{inter} = U_{non-bonded} = U_{LJ} = 4\varepsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right]$$

	CH <sub>3</sub>		CH <sub>2</sub>		S	
	$\varepsilon/k_B[K]$	$\sigma[\text{\AA}]$	$\varepsilon/k_B[K]$	$\sigma[\text{\AA}]$	$\varepsilon/k_B[K]$	$\sigma[\text{\AA}]$
<b>Pool <i>et al.</i></b> JPC 2007	108	3.76	56	3.96	<b>126</b>	<b>4.45</b>
<b>Hautman <i>et al.</i></b> JCP 1989	88.1	3.905	59.4	3.905	<b>200</b>	<b>4.25</b>
<b>Siepmann <i>et al.</i></b> Langmuir 1993	88.1	3.905	59.4	3.905	<b>200</b>	<b>4.97</b>
Lal <i>et al.</i> JPC 2004	98	3.75	46	3.95	126	4.45
Lubna <i>et al.</i> JPC 2005	98	3.75	46	3.95	232	3.62

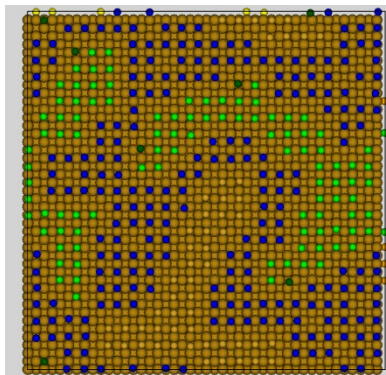
## 6. Perspectives

# Simulation of planar Au(111) & Au(100) surfaces for three models

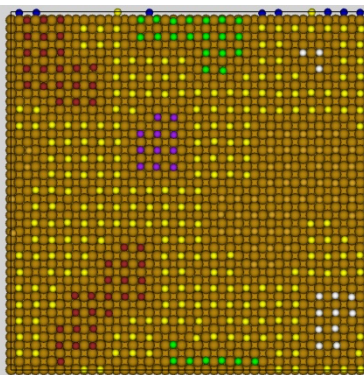


(100)

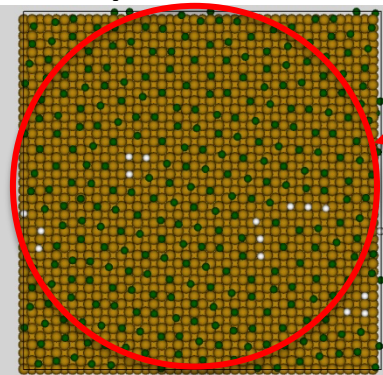
Hautman *et al.*



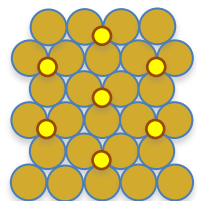
Pool *et al.*



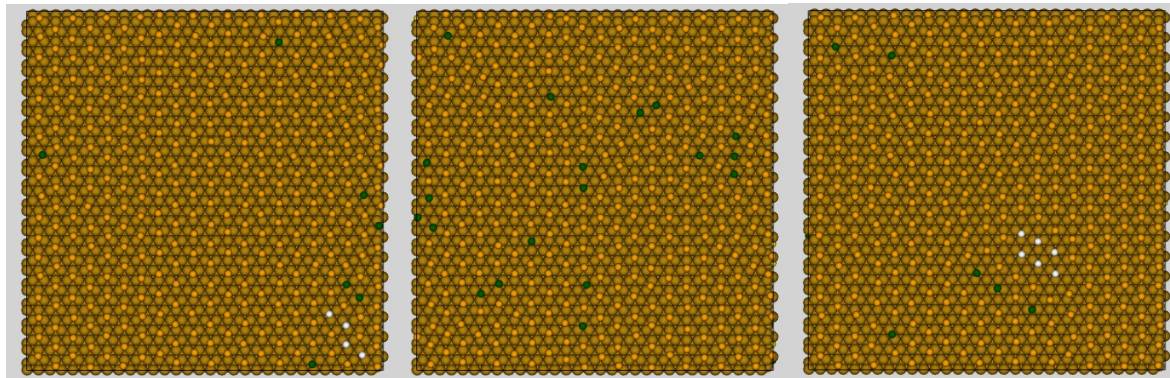
Siepmann *et al.*



Different molecular organization



(111)



Planar surface

Hautman *et al.*

Pool *et al.*

Siepmann *et al.*

Experiment

Au(100)

$19.9 \pm 0.6$

$21.0 \pm 0.6$

$25.1 \pm 0.8$

$20.6^1$

Au(111)

$20.7 \pm 0.6$

$21.2 \pm 0.6$

$22.3 \pm 0.7$

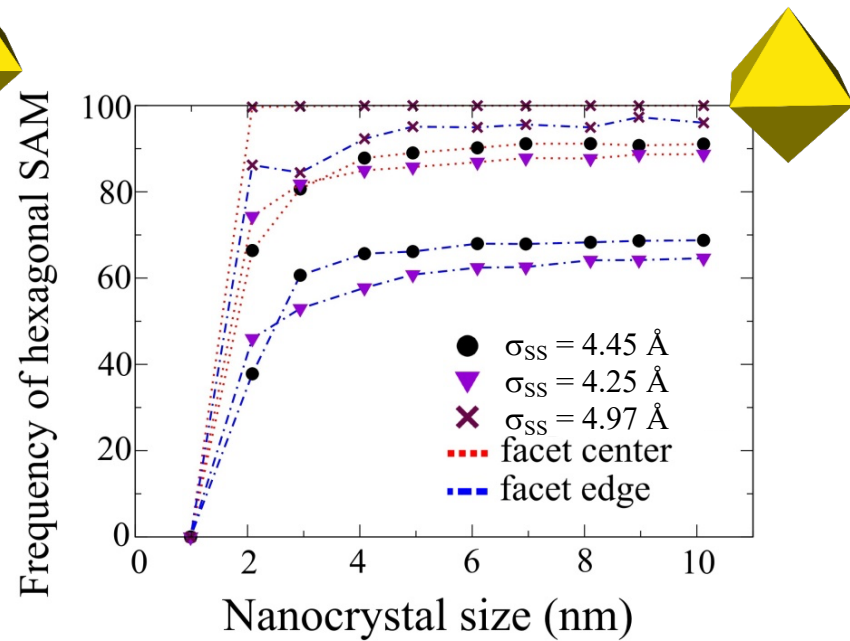
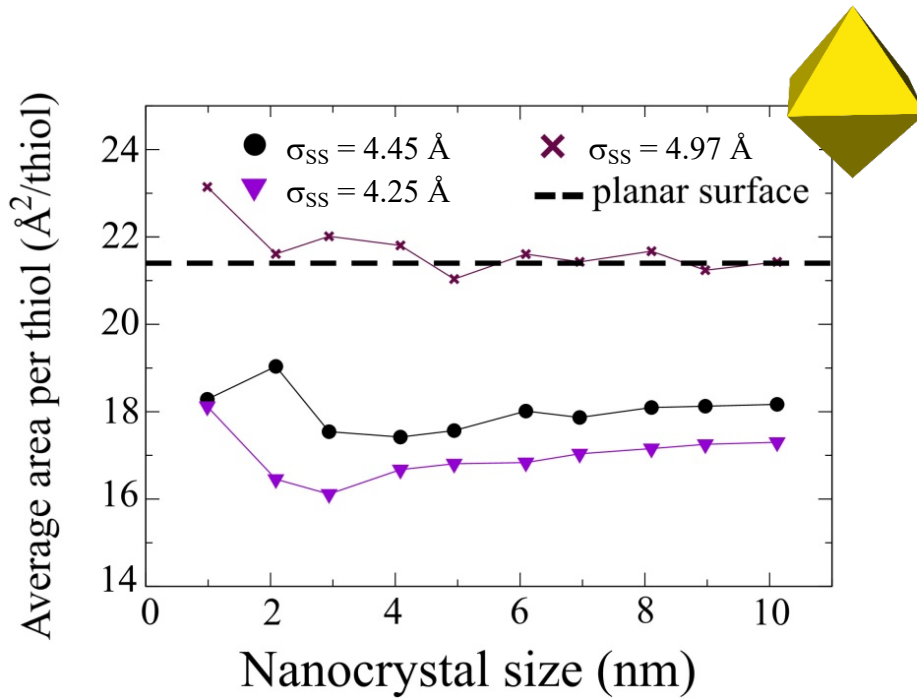
$21.4^1$

Pool *et al.* → closest to experimental results.



# Simulation of Nanocrystals for three models

Siepmann model works for Au(111) surfaces,  
Will it also work for nanocrystals with Au(111) facets? NO

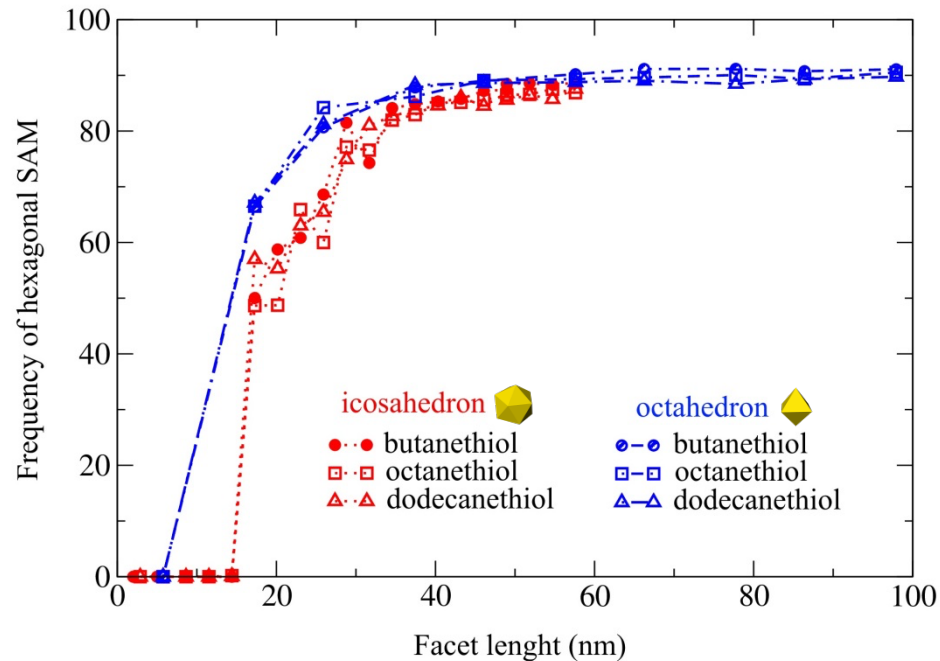


No change of surface coverage with Siepmann model  
Second zig-zag organization disappears on edges.

Interaction models have to be carefully tested.

## Frequency of hexagonal SAMs

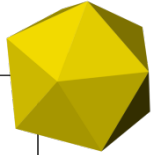
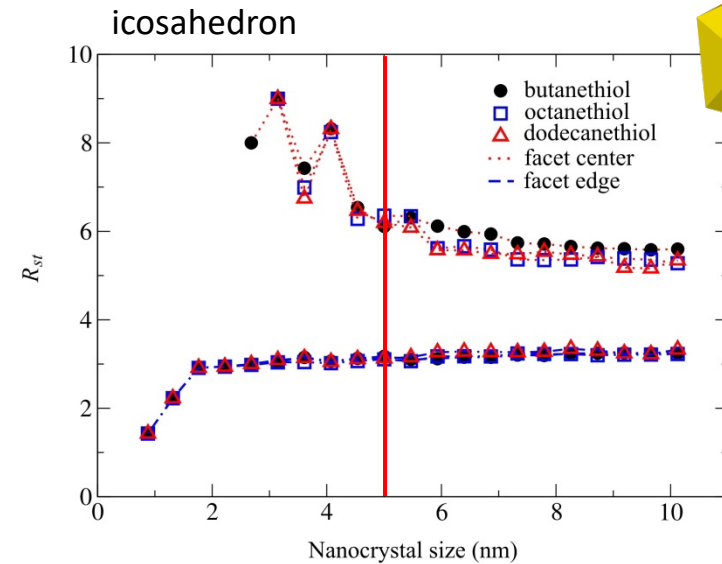
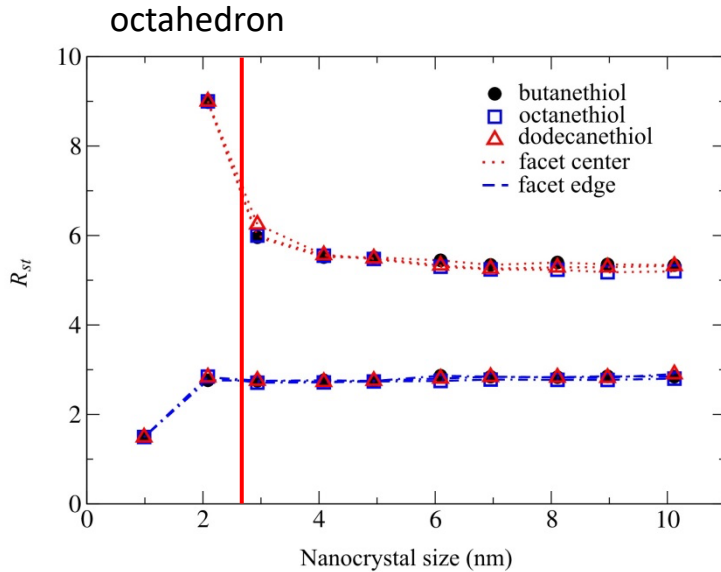
How can we explain the difference between octahedral & icosahedral for NCs < 5 nm ?



→ due to larger facets for octahedral NCs.

### 3. Thiols adsorption simulations - octahedron vs icosahedron

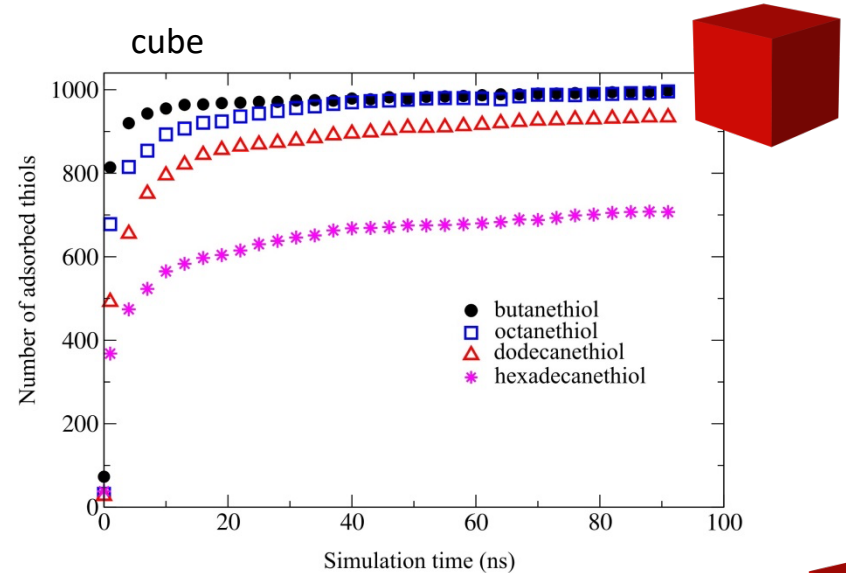
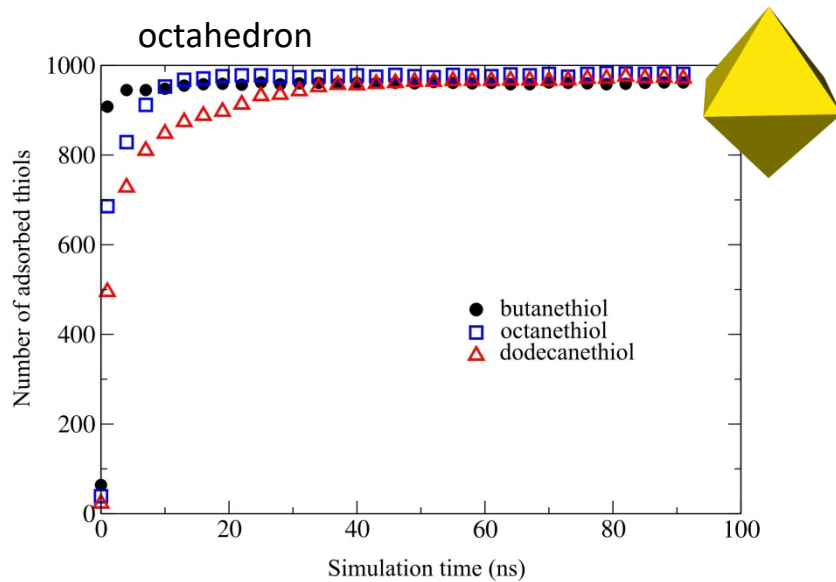
## Ratio between adsorption sites and adsorbed thiols $R_{st}$



- Same constant  $R_{st}$  on the facets edges (facet angle effect).
- $R_{st}$  in the facets centers stabilizes around 6 for octahedral NC > 2 nm, and for icosahedral NC > 5 nm.

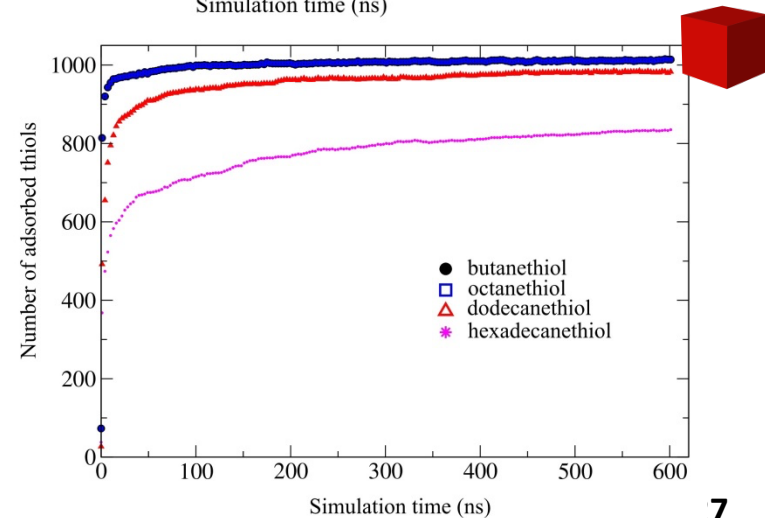
### 3. Thiols adsorption simulations - octahedron vs cube

## Time evolution of thiol adsorption on 7 nm NCs



For cube NCs:

- Slow convergence compared to octahedral & icosahedral NCS.
- Limited accuracy for dodecanethiol results, even after 600 ns.



## 4. Nanocrystals in superlattices

BCC or FCC ?

In experiments<sup>1</sup> : transition FCC → BCC for  $\lambda = 0.8$

$$\lambda = 2L/d_{NC}$$

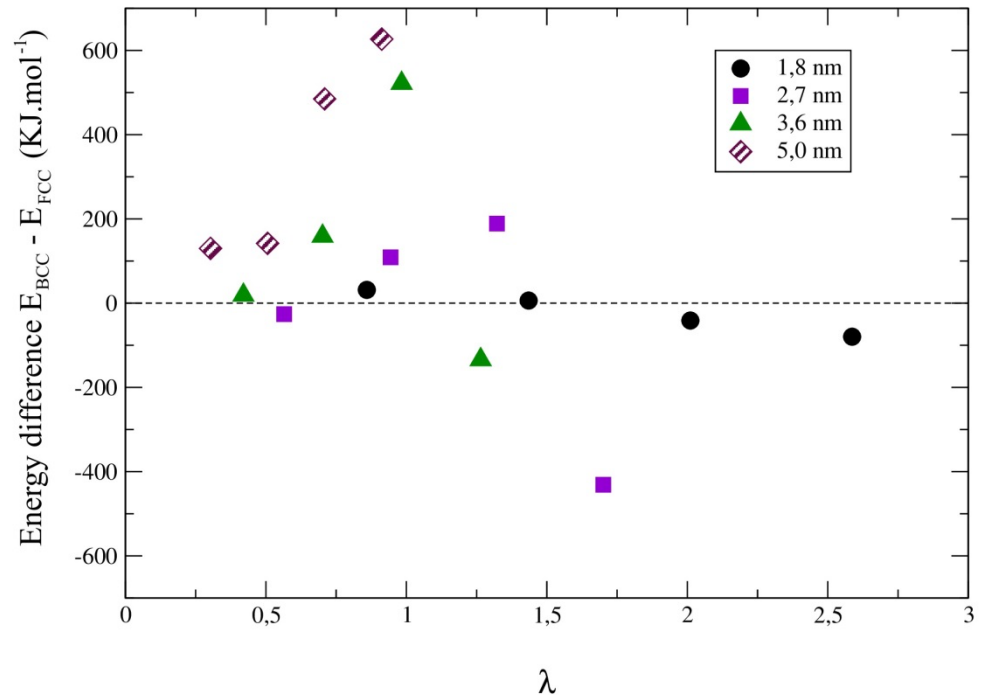
$L$ : ligand chain length

$d_{NC}$ : NC diameter

Approximation



neglect of entropy



Transition FCC → BCC for  $\lambda > 1.0$

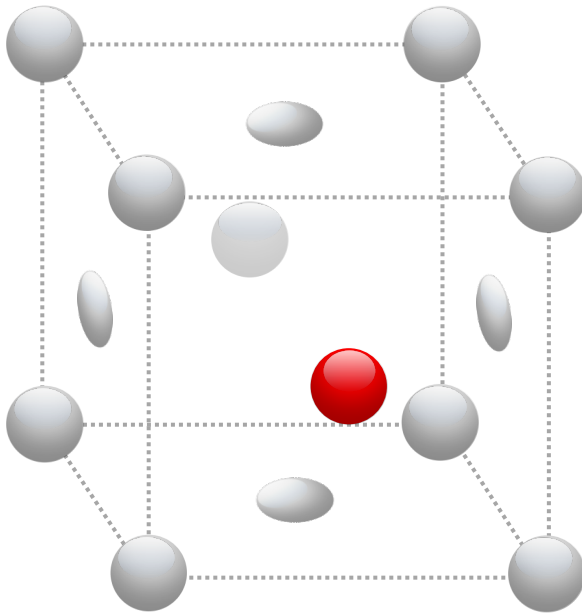


## 4. Nanocrystals in superlattices

BCC or FCC ?

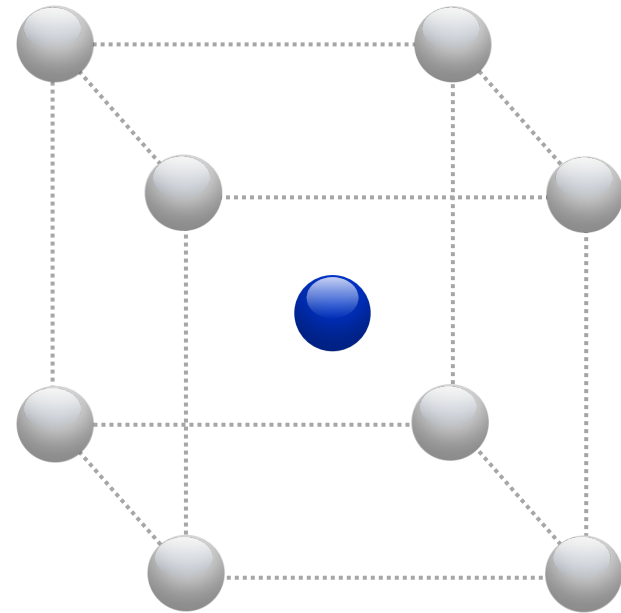
Where does the transition from FCC to BCC come from?

FCC



12 first neighbors

BCC



8 first neighbors  
14 second neighbors

## BCC or FCC ?

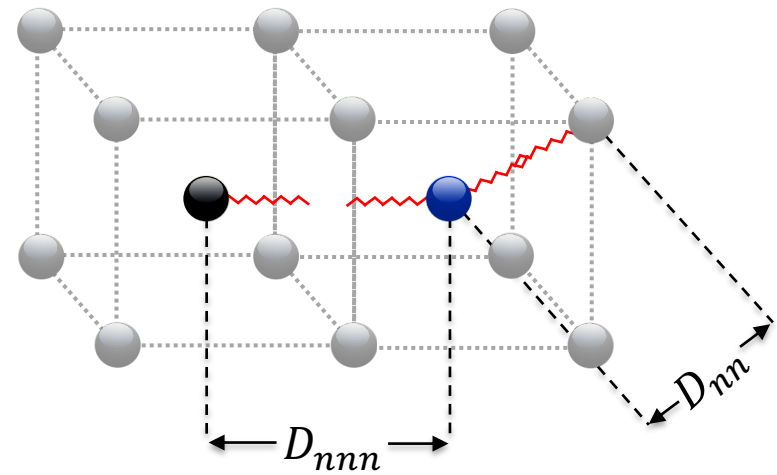
Where does the transition from FCC to BCC come from?

Idea in the literature<sup>1</sup> :

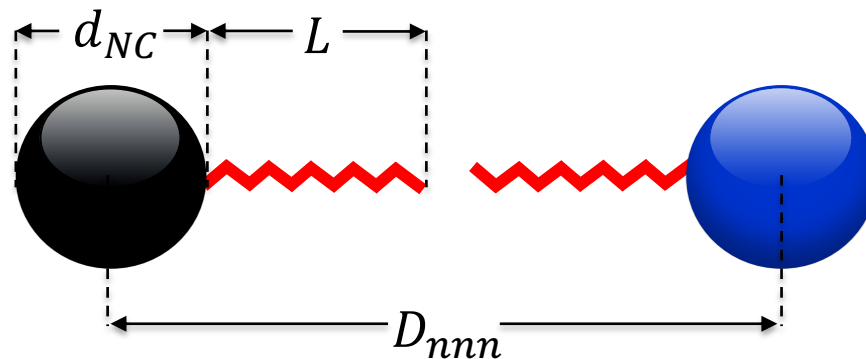
For BCC, the coating of the second neighbors can touch when  $\lambda > 0.8$

Second neighbor contact (BCC)

$$(D_{nnn} - d_{NC}) - 2L \leq 0$$



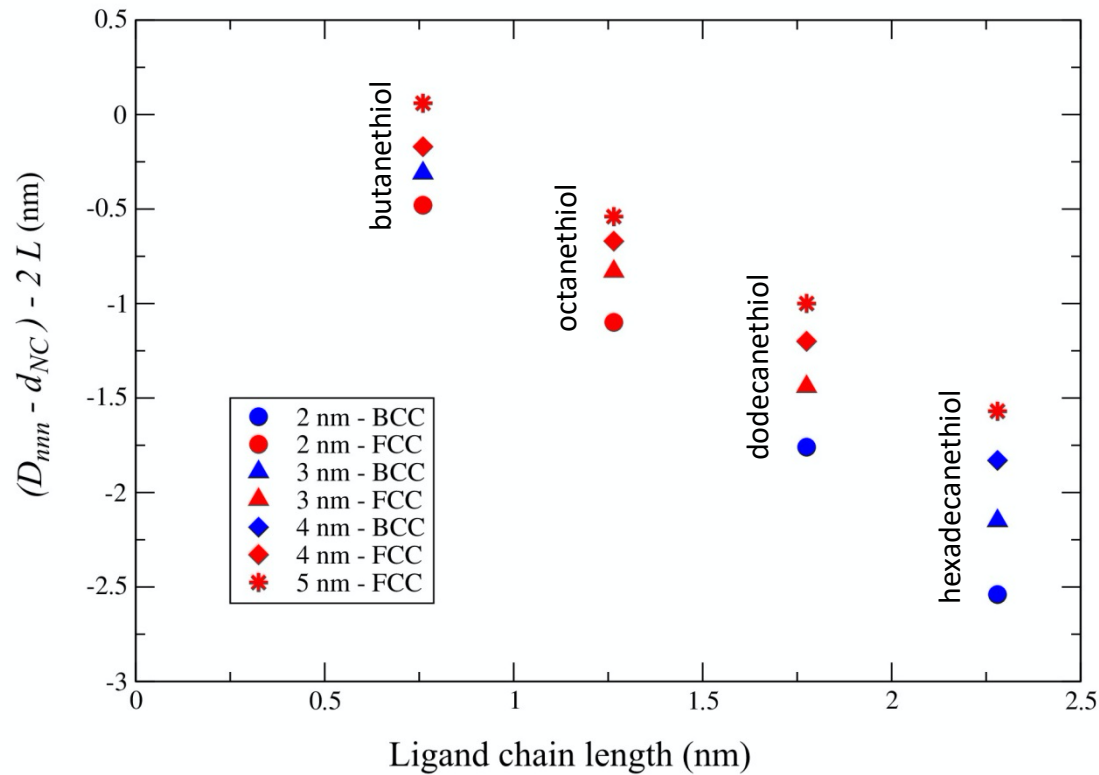
$$D_{nnn} = \frac{\sqrt{2}}{3} D_{nn}$$



## 4. Nanocrystals in superlattices

BCC or FCC ?

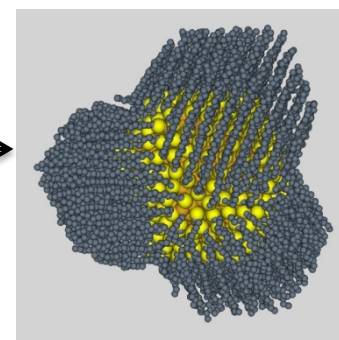
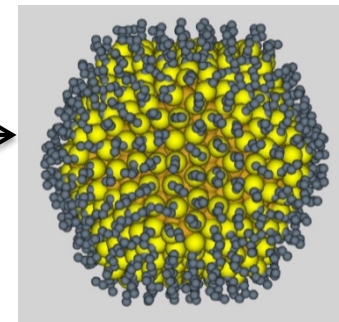
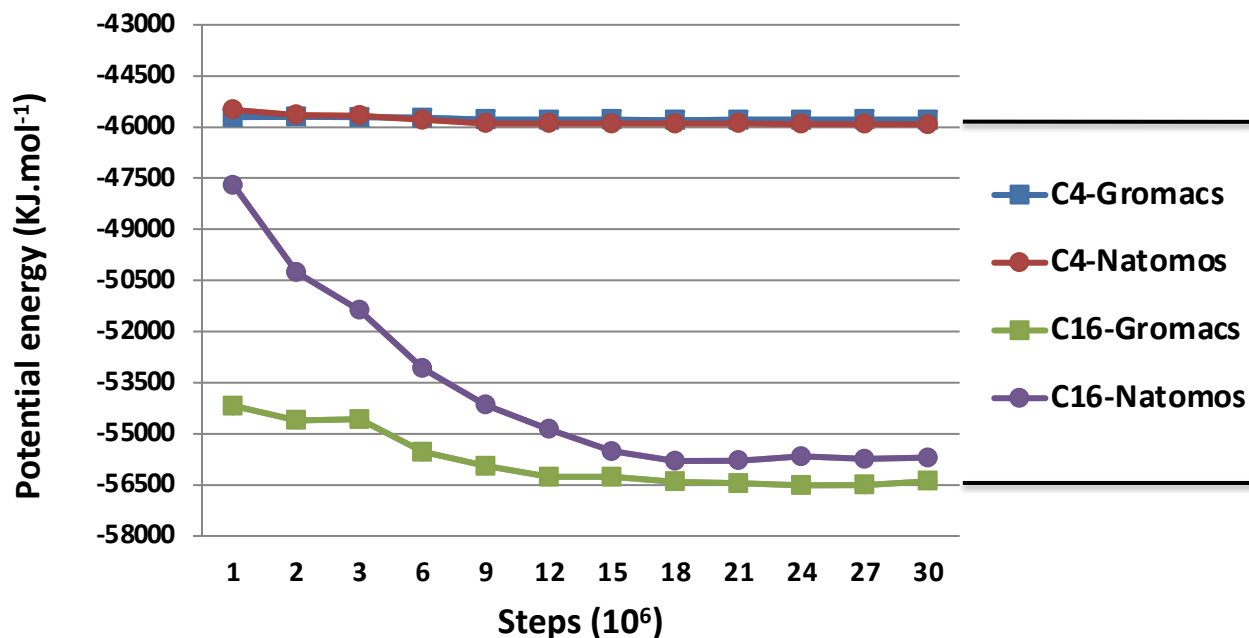
Second neighbor contact



Strong second neighbor contact → BCC.

## 2. Simulation method

### Evolution of potential energy



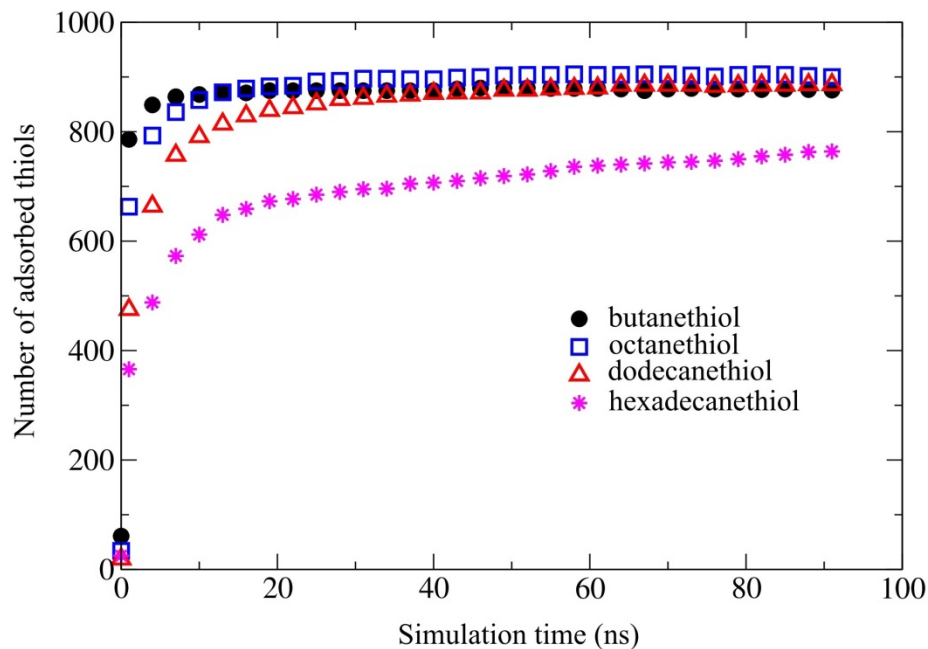
Gromacs simulations converge more rapidly than Natomos

		Energy (KJ.mol <sup>-1</sup> )		Time for 3x10 <sup>6</sup> steps		Ratio	
		Natomos	Gromacs	Natomos 1 CPU	Gromacs 10 CPU		
NC size	2 nm	C <sub>4</sub>	-5995.60	-5994.33	250 min	15 min	<b>15</b>
		C <sub>16</sub>	-6646.44	-7012.62	1070 min	40 min	<b>25</b>
	5 nm	C <sub>4</sub>	-45921.97	-45783.20	60 h	2.1 h	<b>30</b>
		C <sub>16</sub>	-55703,76	-56391.90	250 h	3.2 h	<b>80</b>

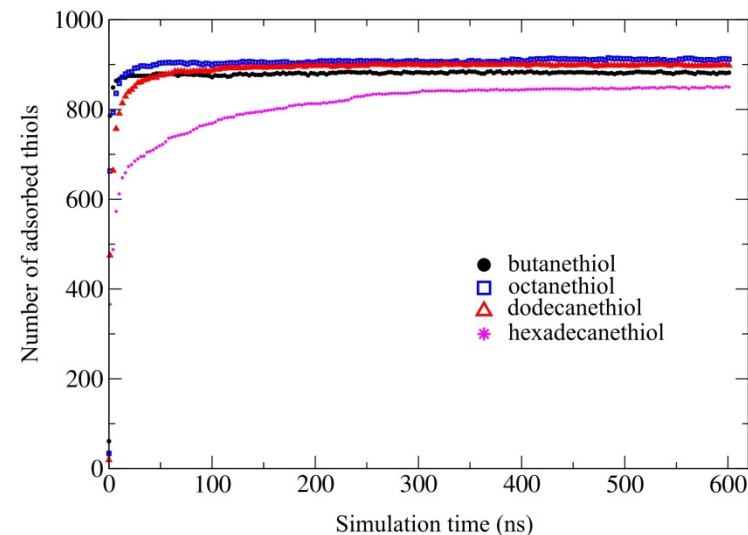
Acceleration of simulation time by a factor up to 400

## Time evolution of thiol adsorption on 7 nm NCs

Is the simulation time sufficiently long ?

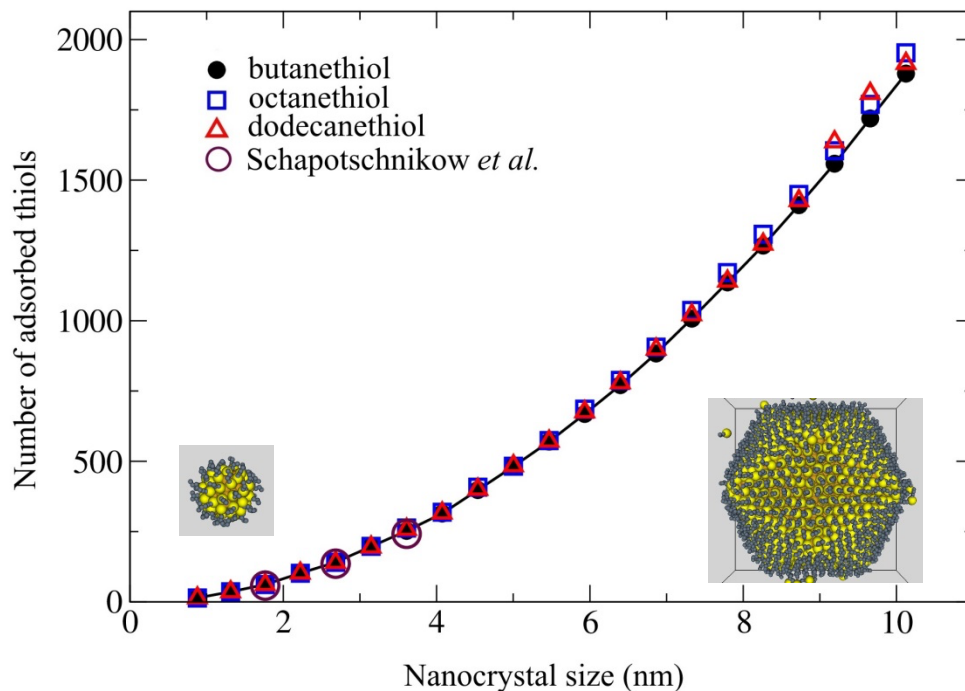


Thiol adsorption simulation  
error :  $\pm 1\%$



- Time evolution of thiol adsorption depends on the thiol chain length.
- Adsorption convergence is very slow for hexadecanethiol even after 600 ns  
→ no further simulations.

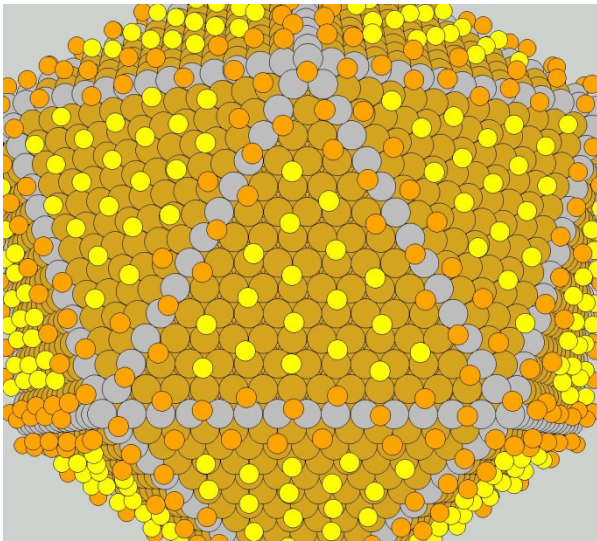
## Number of adsorbed thiol molecules



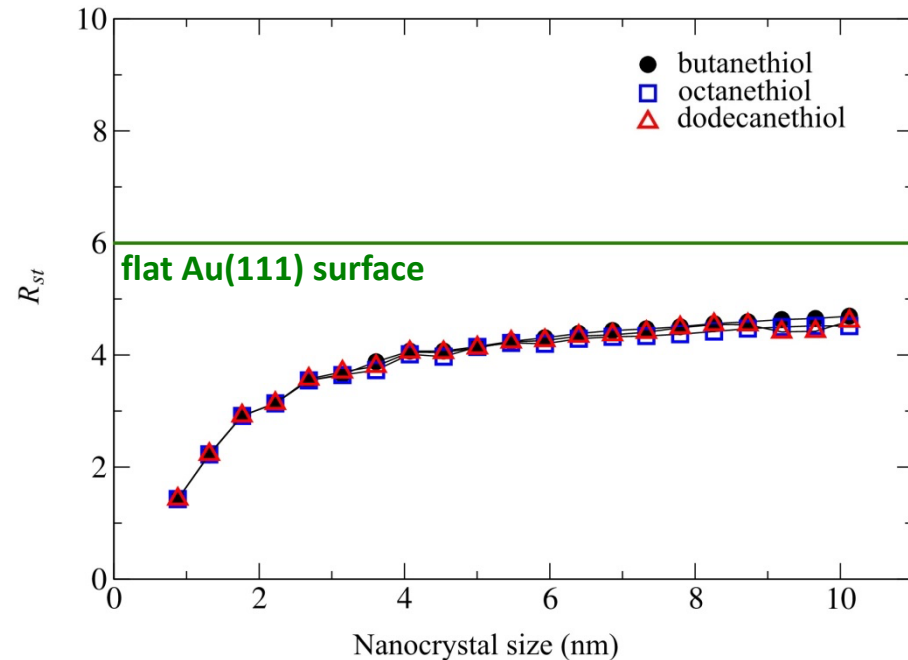
- the number of adsorbed thiols depends only slightly on the alkane chain length.
- In good agreement with simulation results in the literature<sup>1</sup> (same interaction model).

## Ratio between adsorption sites and adsorbed thiols

- $R_{st}$  = number of adsorption sites / number of adsorbed thiols.
- $R_{st} = 6$  for planar Au(111) surface. Will we find  $R_{st} = 6$ ?



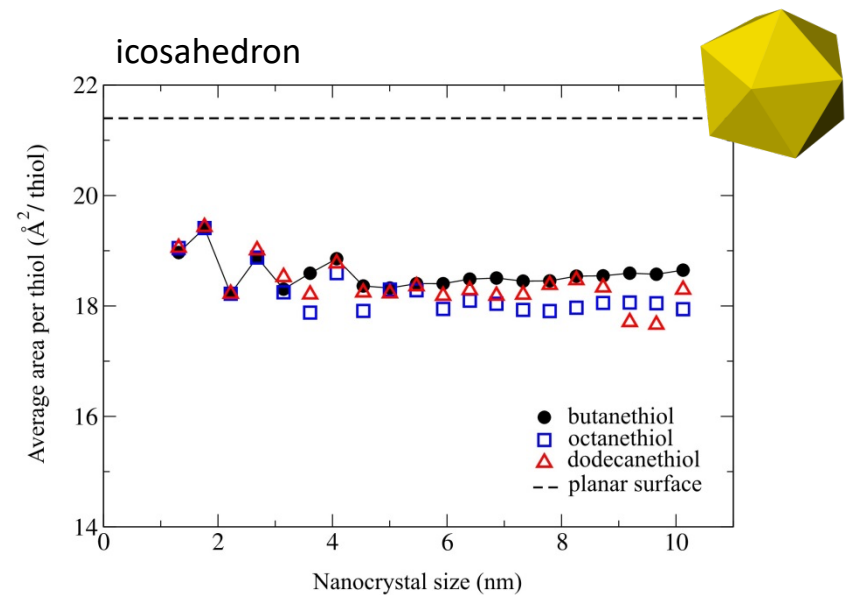
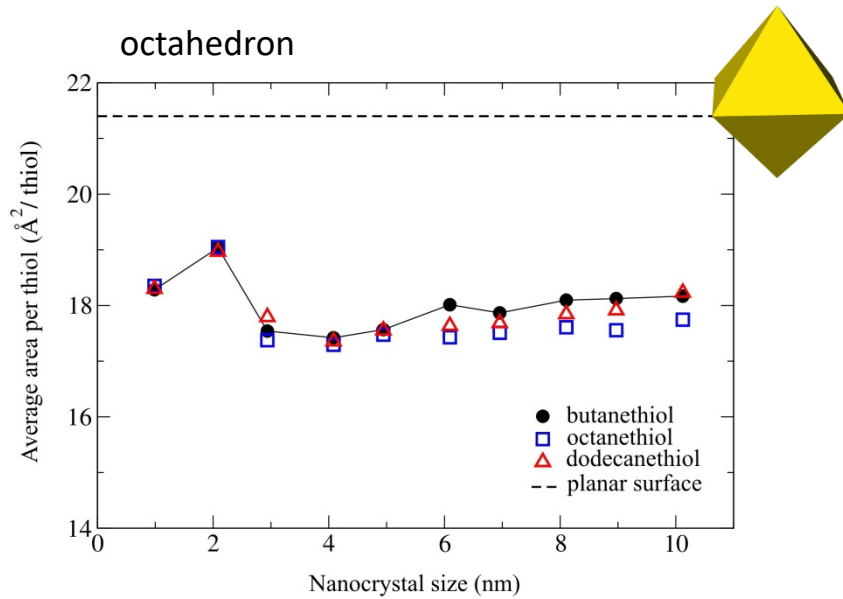
Positions of SH groups on a nanocrystal facet



- Total  $R_{st} < 6$  (value for planar Au(111) surface).

### 3. Thiols adsorption simulations - octahedron vs icosahedron

## Average area per thiol

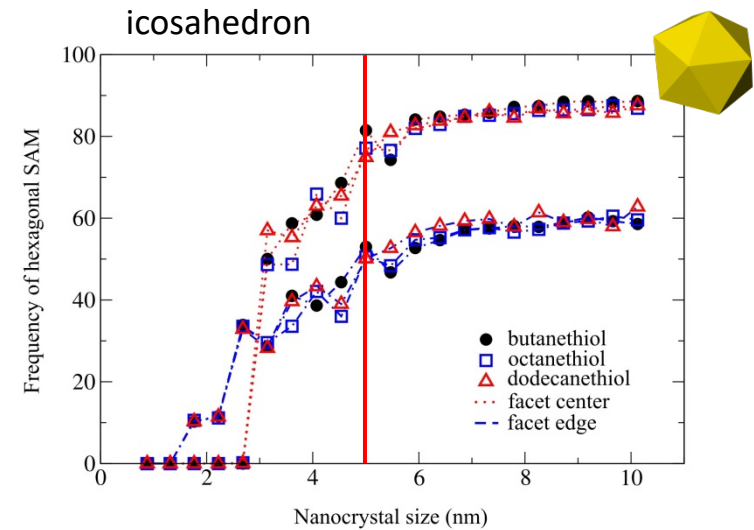
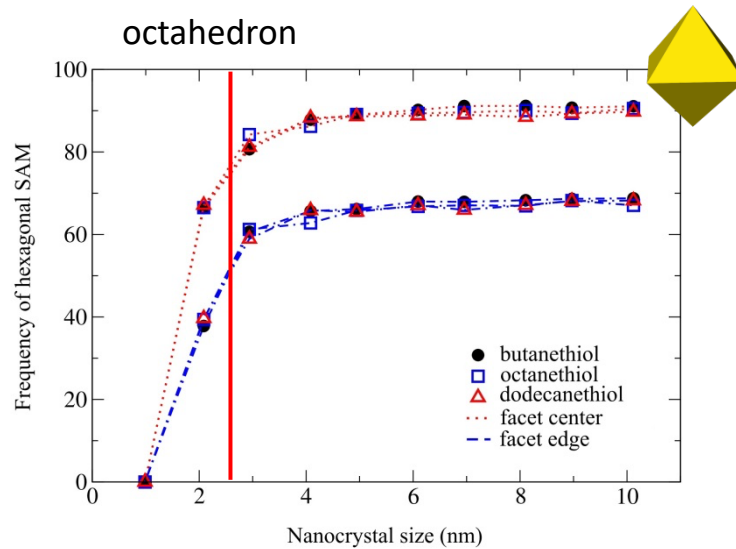


- Similar results for octahedral & icosahedral NCs.



### 3. Thiols adsorption simulations - octahedron vs icosahedron

## Frequency of hexagonal SAMs

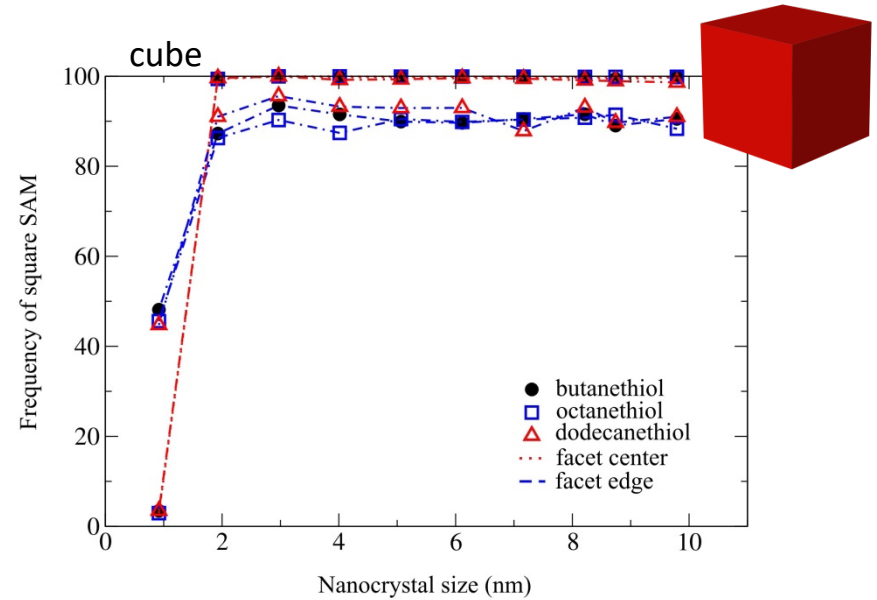
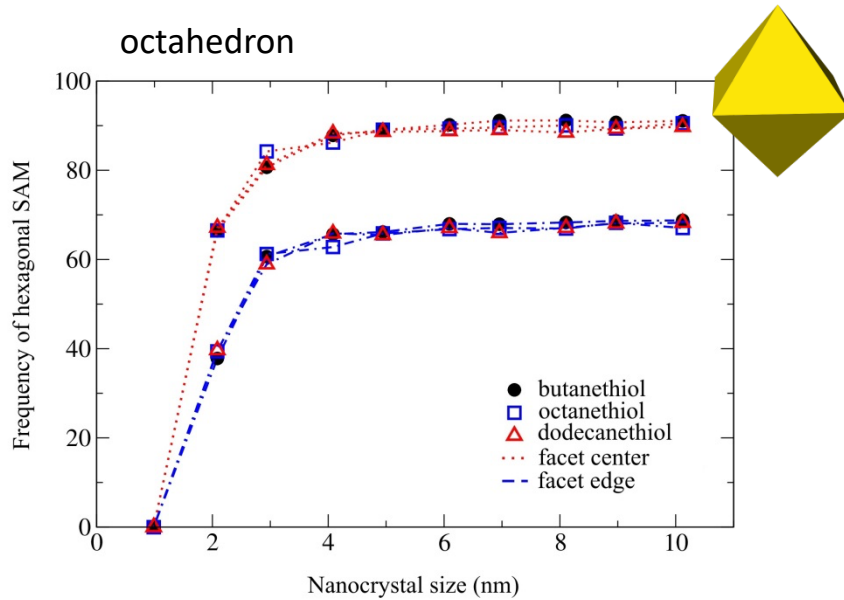


Octahedral NCs reach behaviour of Au(111) for smaller nanocrystals.

At a given nanocrystal size, the facets are larger.

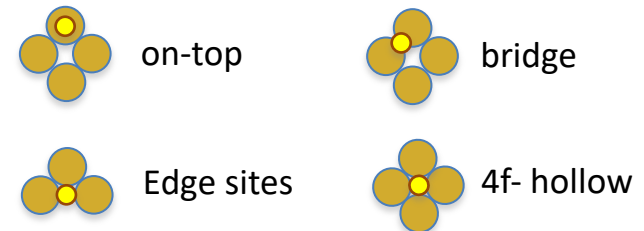
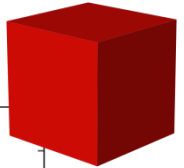
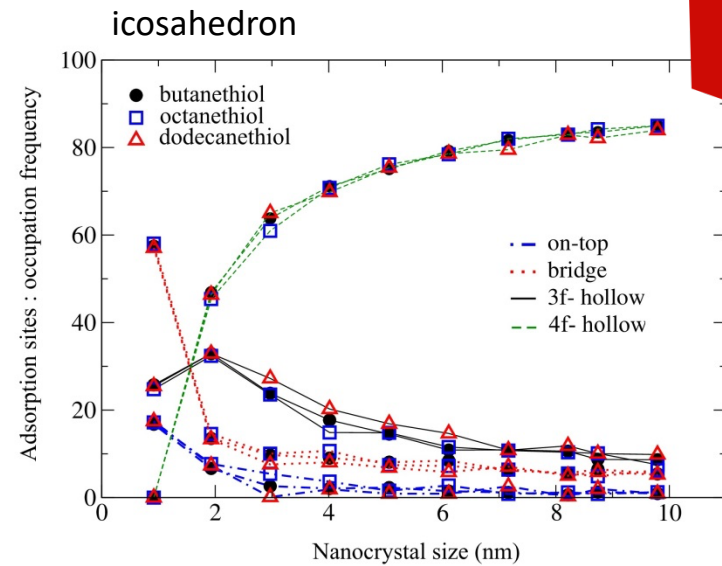
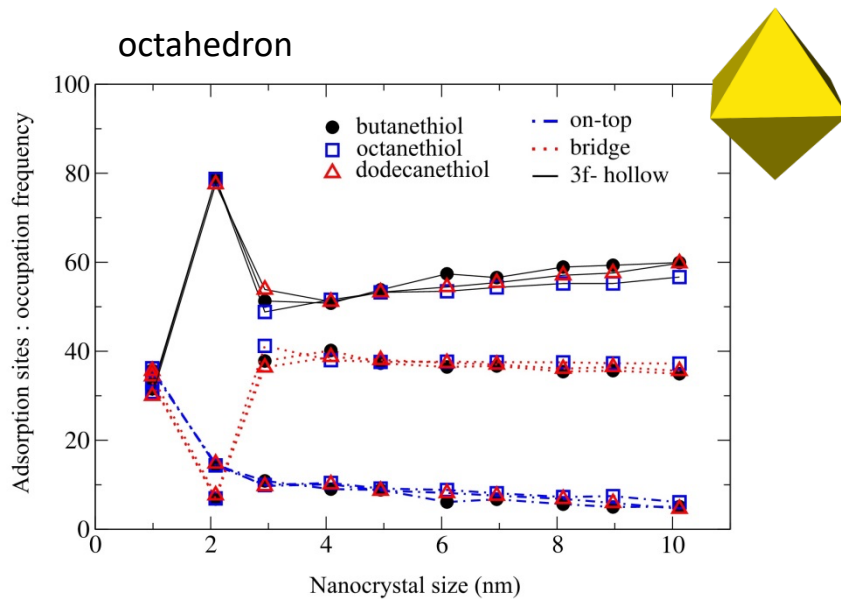
### 3. Thiols adsorption simulations - octahedron vs cube

## Frequency of hexagonal & square SAM



Square SAM frequencies confirm the same molecular organization on (100) facet center & edges.

## Adsorption sites : occupation frequencies



- Octahedron : 3f- hollow & shifted bridge adsorption site.
- Cubes : mainly 4f- hollow adsorption site: **Slow saturation due to edge sites.**