Non covalent interactions

Real space point of view



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Outline

- Why are we still studying NCIs?
- QTAIM (Quantum Theory of Atoms in Molecules)
 - Critical points
 - Integrals
- NCI (Non covalent interaction index)
 - Definition
 - NCI vs AIM
 - Big systems
- Summary

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Motivation

Why?

Covalent bonds: easy to represent



- The binding energy well is very steep
- Easy to parametrize

Motivation

Why?

Covalent bonds: easy to represent



- The binding energy well is shallow (much more non local too!)
 - Less directional
 - Interactions between many atoms...
- This makes it more difficult to detect, calculate, model, add, ...

Motivation

Weak interactions are critical for:

- states of matter, water properties, solubility,
- surface chemistry,
- nano-scale and materials chemistry,
- biological chemistry
 - protein folding,
 - ligand-receptor binding,
 - drug interactions







- Quantum mechanical information in 3D... electron density!
 - $\rho(\mathbf{r})$ is a fundamental property of any electronic system $\rho(\vec{r}) = N \int ... \int |\Psi(\vec{x}_1, \vec{x}_2, ..., \vec{x}_N)|^2 ds \, d\vec{x}_2 ... \vec{x}_N$
 - is experimentally accessible
 - is defined within the exact many-body theory,
 - is supported by the Hohenberg–Kohn theorem

QTAIM: From electronic density to chemical structure



Density

•Maxima = nuclei



QTAIM: From electronic density to chemical structure



- •Maxima = nuclei
- Bond = 1st order saddle point (*bcp*)

IMPORTANT PROPERTIES

- Each maximum has an associated region of space (basin)
 - Non overlapping
 - They fill up the volume



Each maximum has an associated region of space (basin)

- Non overlapping
- \succ They fill up the volume
- Have a chemical meaning

We can integrate properties!



The topology of the density alone is not able to provide a satisfactory picture of **weak bonds**



Pair interactions are not well described by critical points

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If the profile is flat...

Let's look at the region $\nabla \rho \to 0$





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NCI:

analysis of the reduced density gradient at low densities

s=
$$\frac{1}{c_s} \frac{|\nabla \rho|}{\rho^{4/3}}$$
 with $c_s = 2(3\pi^2)^{1/3}$





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How does it work?



Non-interacting densities







Non-interacting densities



$$o(x, y, z) = \left(\frac{\zeta^{3/2}}{\sqrt{\pi}}e^{-\zeta\sqrt{x^2 + y^2 + (z-R)^2}}\right)^2$$



Interacting densities $\rho = \left(\int_{-\infty}^{\infty} \frac{1}{\sqrt{\pi}} e^{-\zeta \sqrt{x^2 + y^2 + (z - R/2)^2}} \right)^2 + \left(\int_{-\infty}^{\infty} \frac{1}{\sqrt{\pi}} e^{-\zeta \sqrt{x^2 + y^2 + (z + R/2)^2}} \right)^2$

 $s(\rho) \propto \rho^{-1/3} \xrightarrow{\rho \to 0} \infty$

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Interacting densities





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Nevertheless, thanks to the shape of the isosurface we can visually collect more information...



Benzene packing maximizes the number of C-H··· π and C-H···C contacts.

NCI vs AIM

Delocalized interactions

AIM

Largely oriented location of H3 Straight BP privileges the interaction of the H with just one single atom of the ring



NCI **Disc-shaped and localized** H3 conventional, very weak HB

NCI and BP pictures nicely match

NCI vs AIM

Delocalized interactions

AIM

CH…C interaction significantly bent H roughly equidistant to the whole ring



NCI

Large isosurface that covers the ring C-H \cdots π interaction involving the whole π electron cloud



BP analysis privileges the interaction of the H with just one single atom of the ring NCI provides a delocalized interaction

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We don't have a wavefunction!!!



Non covalent interactions are crucial in supramolecular systems...can we apply NCI to them ?

 YES: density approximated from atomic densities (NCI=very little perturbation)



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Non covalent interactions are crucial in supramolecular systems...can we apply NCI to them ?

- YES: density approximated from atomic densities (NCI=very little perturbation)
- Only atomic coordinates are required as input

(x,y,z of atoms, crystallographic coordinates)

 Very fast calculation; applicable to large systems

Big systems



•Hydrogen bonds stabilize the helix

•Big region of van der Waals interaction inside the helix and between methyle lateral chains one step away

Big systems

polypeptide: anti-parallel β -sheet consisting of 17 glycine residues



•Van der Waals interactions between CH₂ groups

Big systems



Summary

- We can locate convalent bonds from the electron density (QTAIM)
- We can locate non-covalent interactions from the reduced density gradient (NCI)
 - It enables to identify delocalized interactions
 - It gives insight into QTAIM blind weak interactions
 - It can be approximated for very big systems with promolecular densities

The programs

NCI for solid calculations PCCP 14, 12165 (2012)

