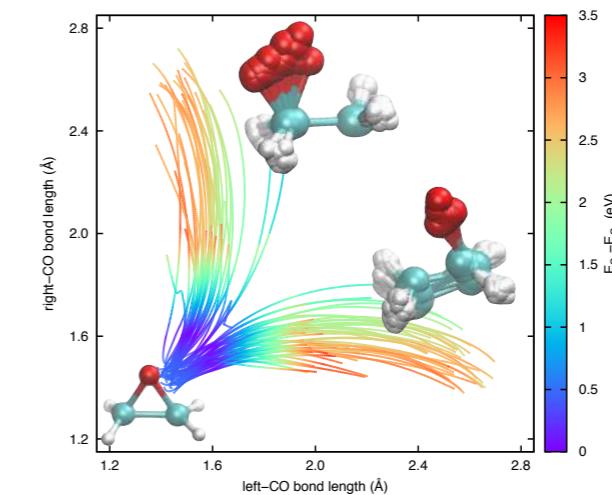
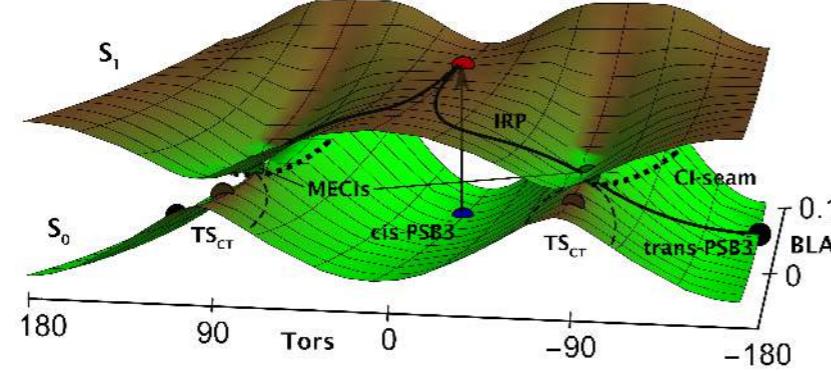


Dynamics of electrons and nuclei in molecules

Beyond the Born-Oppenheimer approximation



Federica Agostini

Institut de Chimie Physique, University Paris-Saclay
Orsay, France

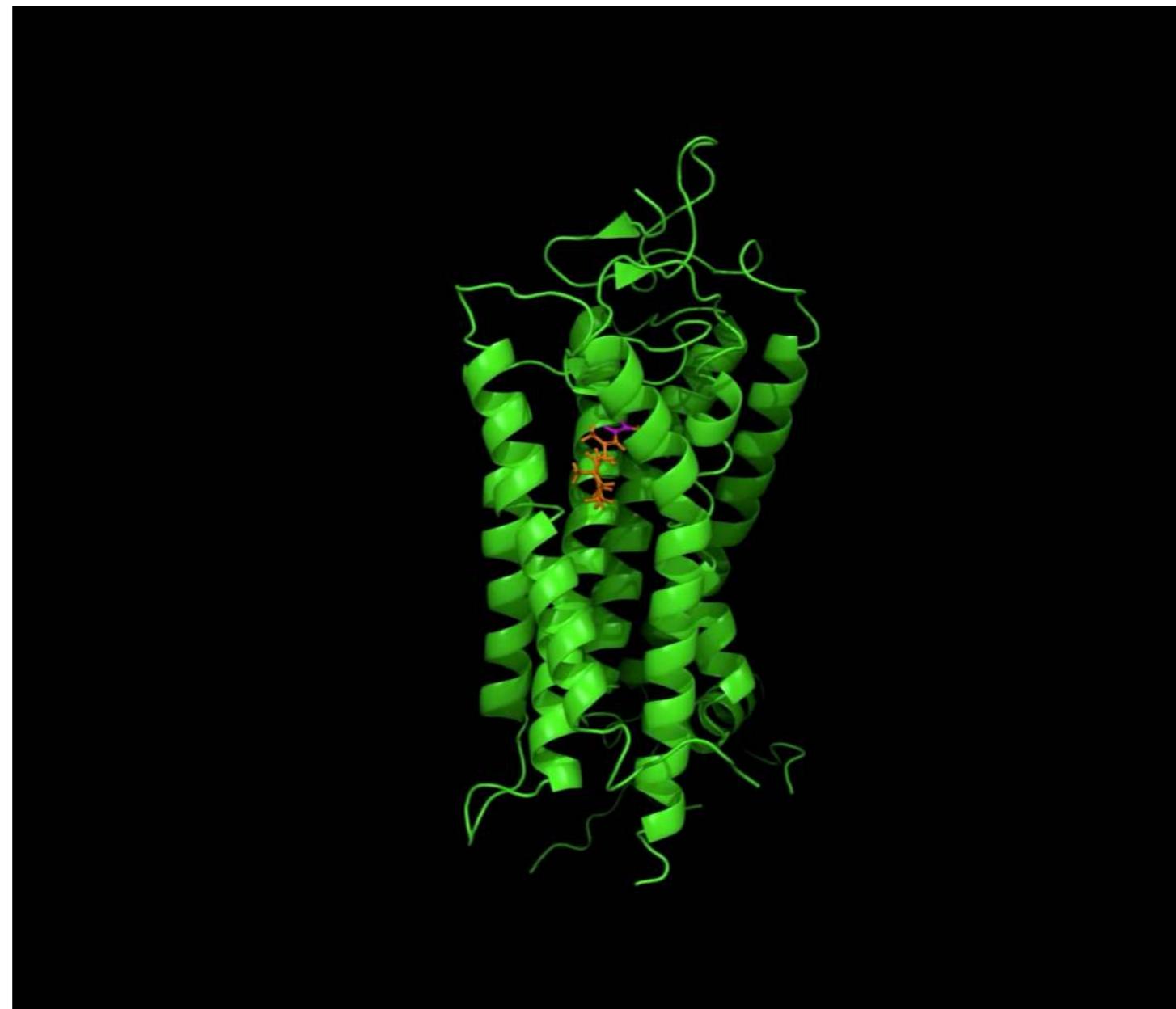
Summary

“N-body” problem (electrons & nuclei) + ultrafast dynamics

- photo-activated ultrafast phenomena in a nutshell
- the quantum-mechanical problem & approximations
- trajectory-based approaches to excited-state dynamics
- exact factorization of the electron-nuclear wavefunction
- an overview on the applications

What happens to a molecule after photo-excitation?

cis-trans isomerization of the retinal chromophore in the rhodopsin protein as the first step in the process of vision



one of the
fastest
photochemical
reactions known
in nature
(200 fs)

theoretical
description need
to go beyond the
Born-
Oppenheimer
approximation

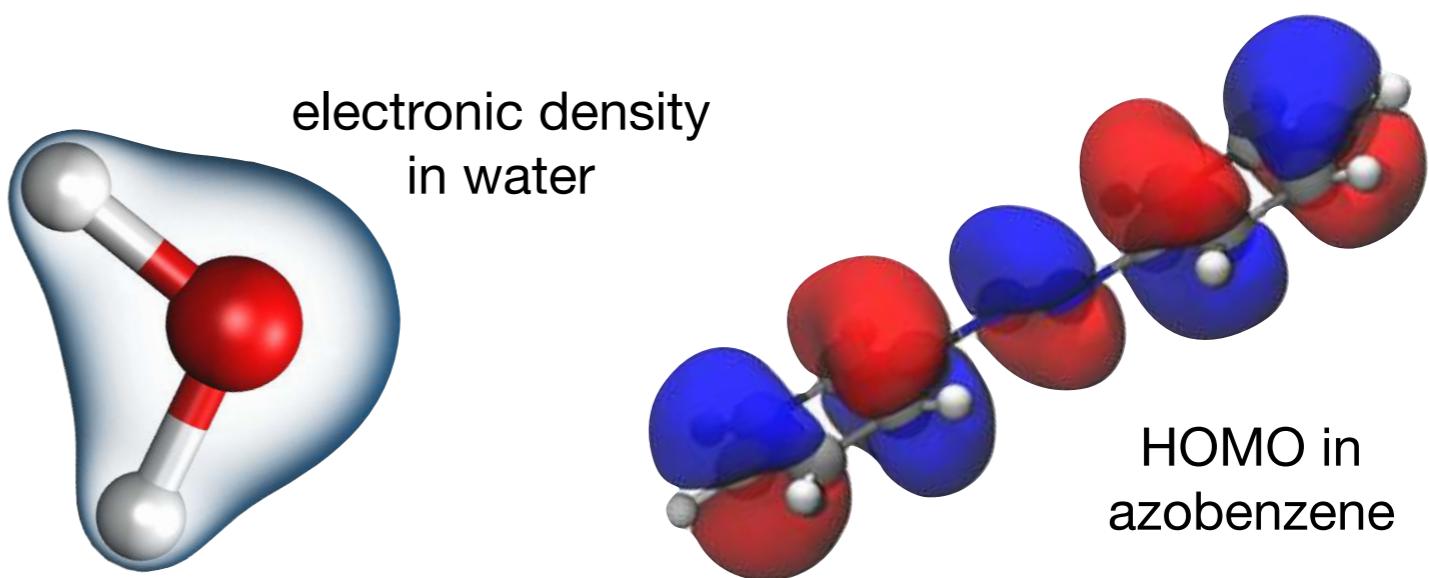
Simulations of light-matter interaction phenomena

systems of interacting
electrons and nuclei

microscopic quantum
mechanical description

electronic excited-state
effects

nuclear quantum
effects



Simulations of light-matter interaction phenomena

systems of interacting
electrons and nuclei

**microscopic quantum
mechanical description**

electronic excited-state
effects

nuclear quantum
effects

$$i\hbar\partial_t\Psi(\mathbf{r}, \mathbf{R}, t) = [\hat{T}_n + \hat{H}_{el}]\Psi(\mathbf{r}, \mathbf{R}, t)$$

Simulations of light-matter interaction phenomena

systems of interacting electrons and nuclei

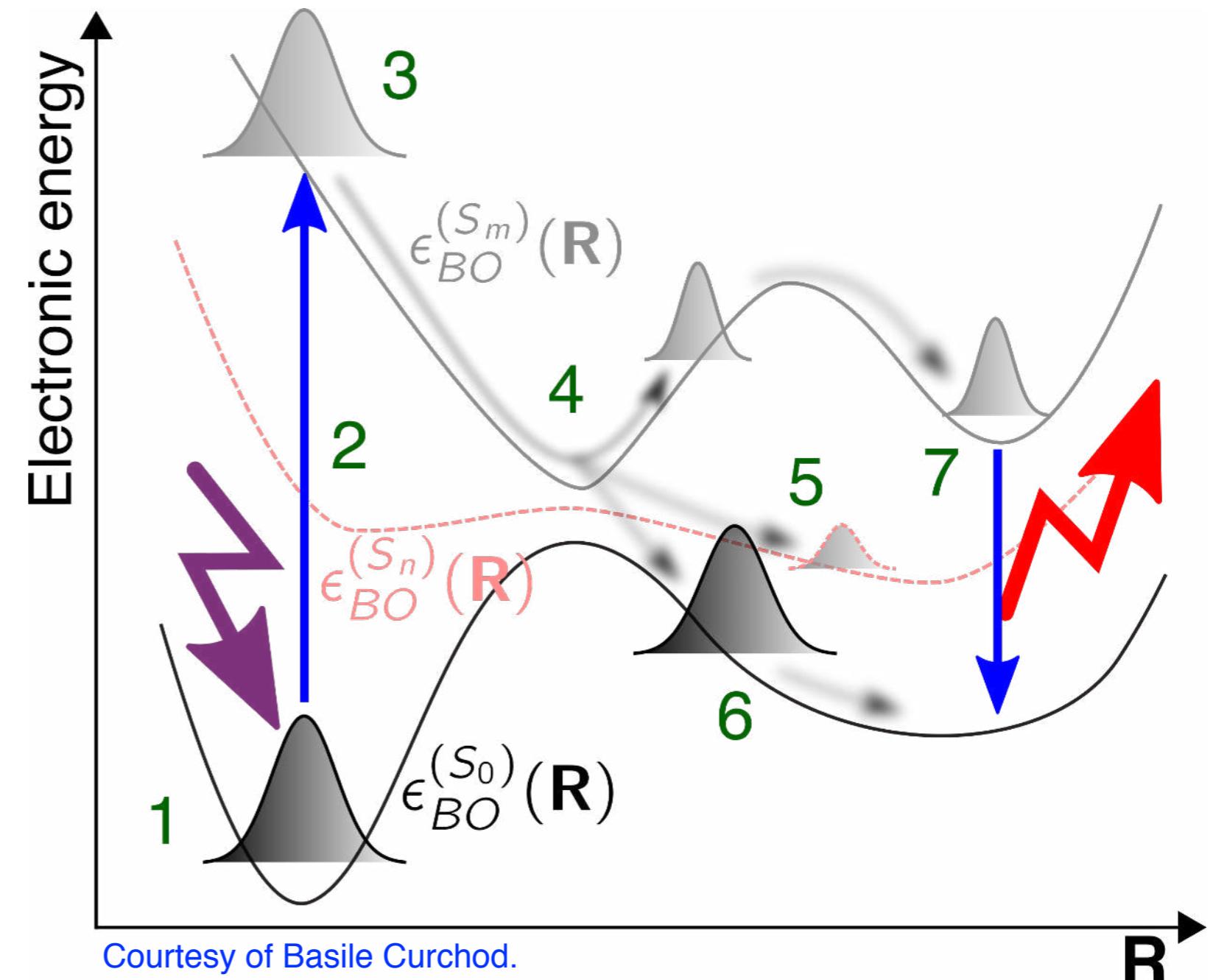
microscopic quantum mechanical description

electronic excited-state effects

quantum chemistry

nuclear quantum effects

nuclear dynamics



Courtesy of Basile Curchod.

$$i\hbar\partial_t\Psi(\mathbf{r}, \mathbf{R}, t) = [\hat{T}_n + \hat{H}_{el}] \Psi(\mathbf{r}, \mathbf{R}, t)$$

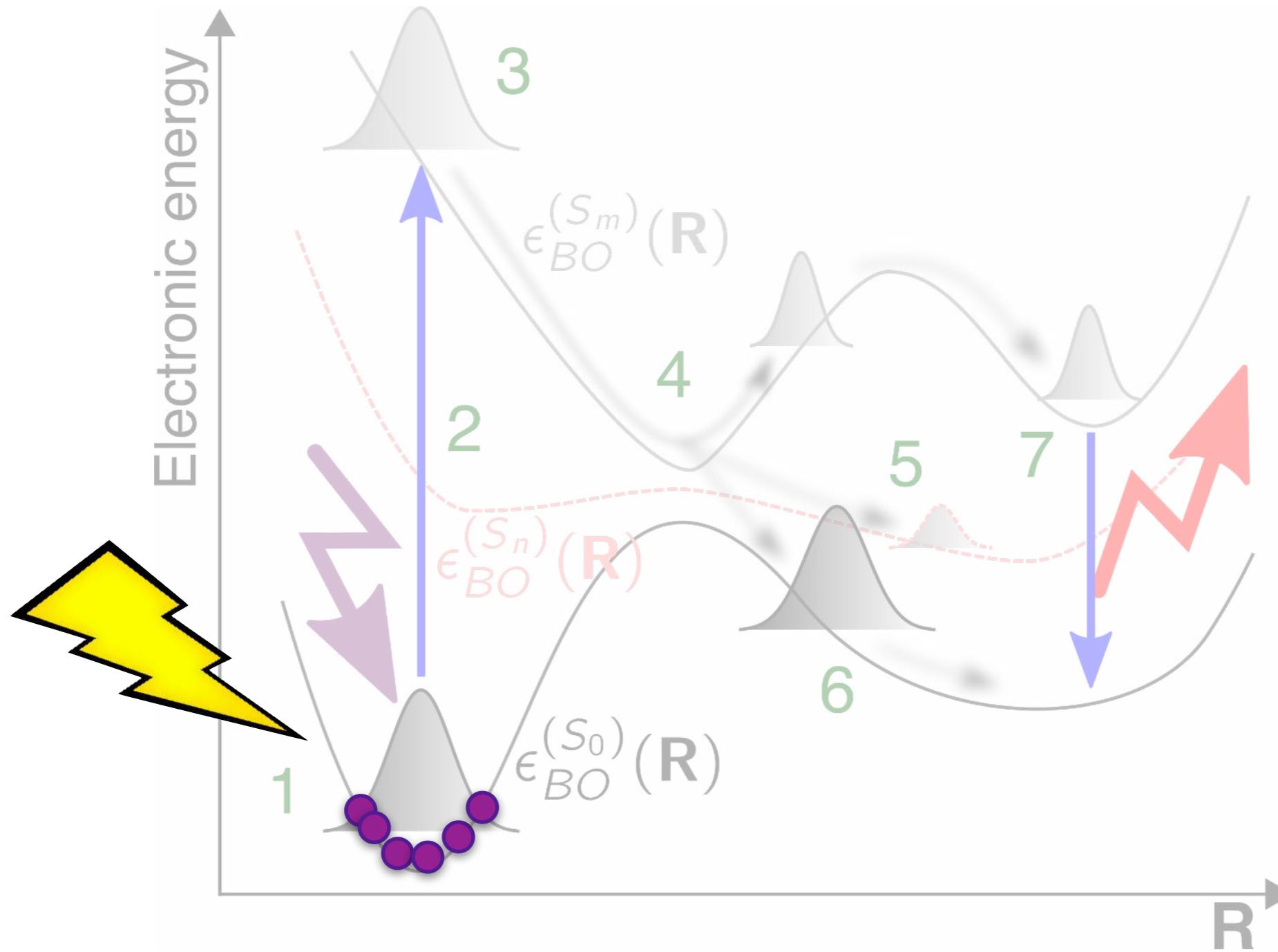
Ab initio molecular dynamics simulations

electronic excited-state effects

nuclear quantum effects

quantum chemistry

nuclear **classical-like** dynamics



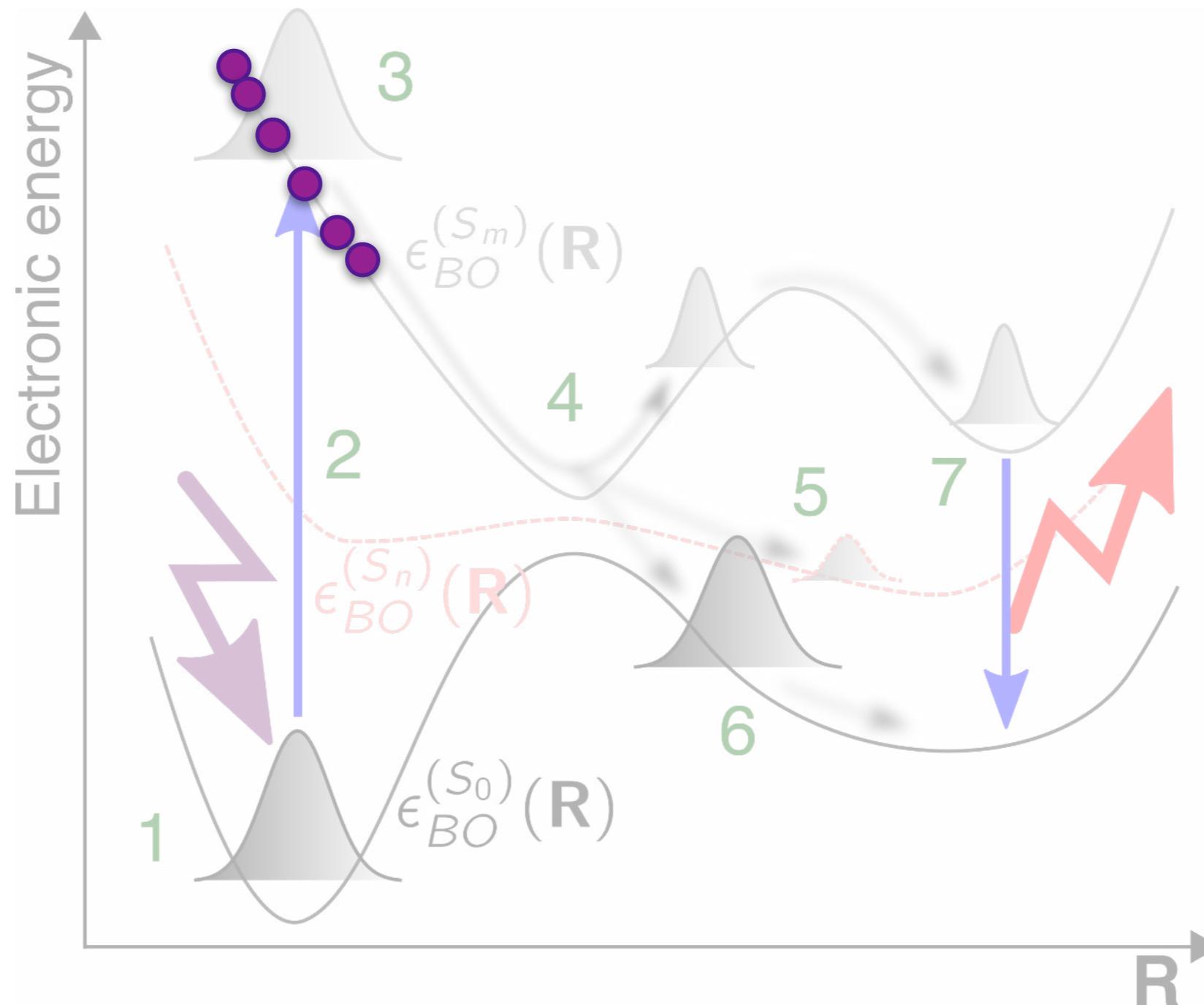
Ab initio molecular dynamics simulations

electronic excited-state effects

quantum chemistry

nuclear quantum effects

nuclear **classical-like** dynamics

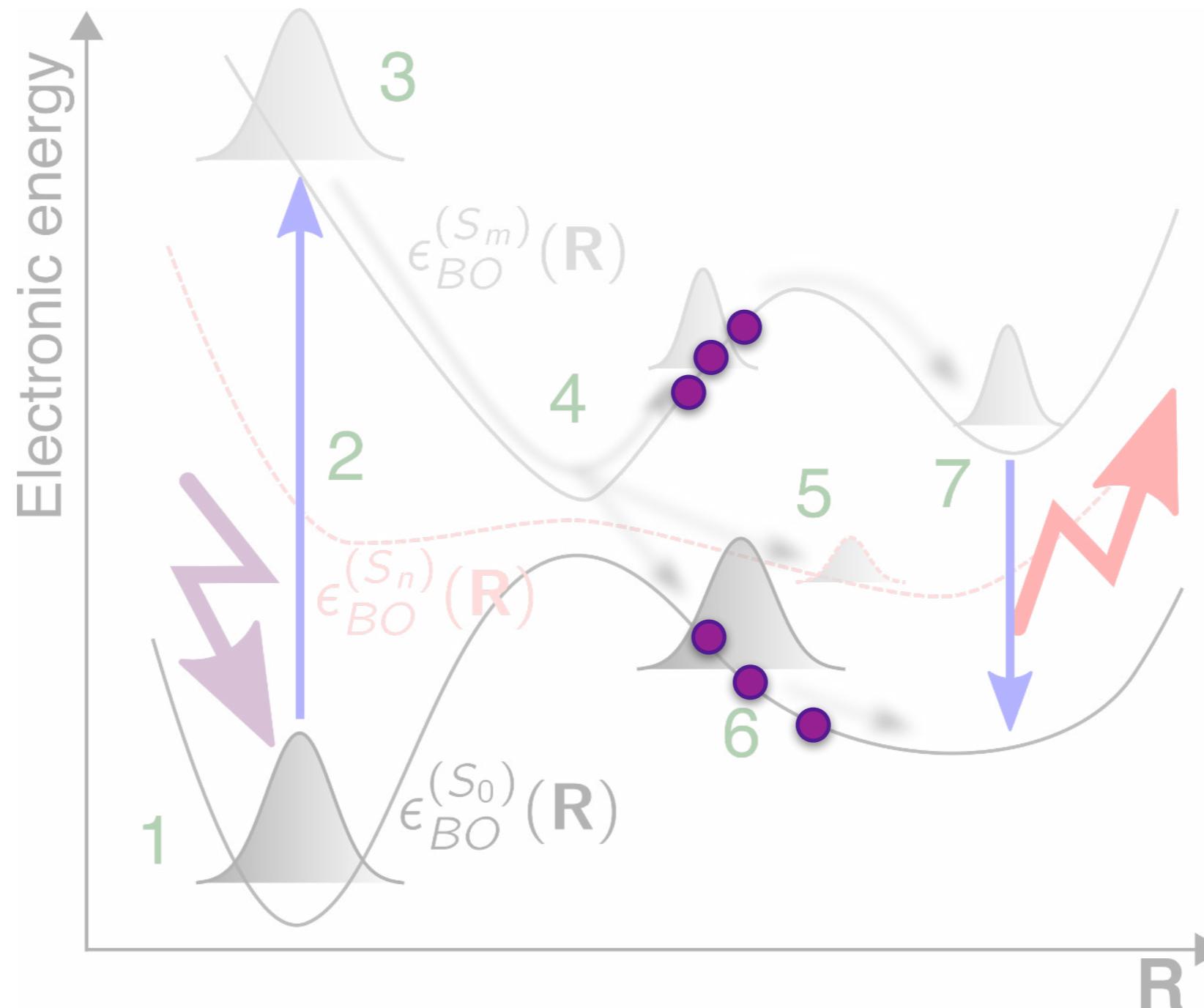


Ab initio molecular dynamics simulations

electronic excited-state effects

nuclear quantum effects

quantum chemistry nuclear **classical-like** dynamics



Ab initio molecular dynamics simulations

electronic excited-state effects

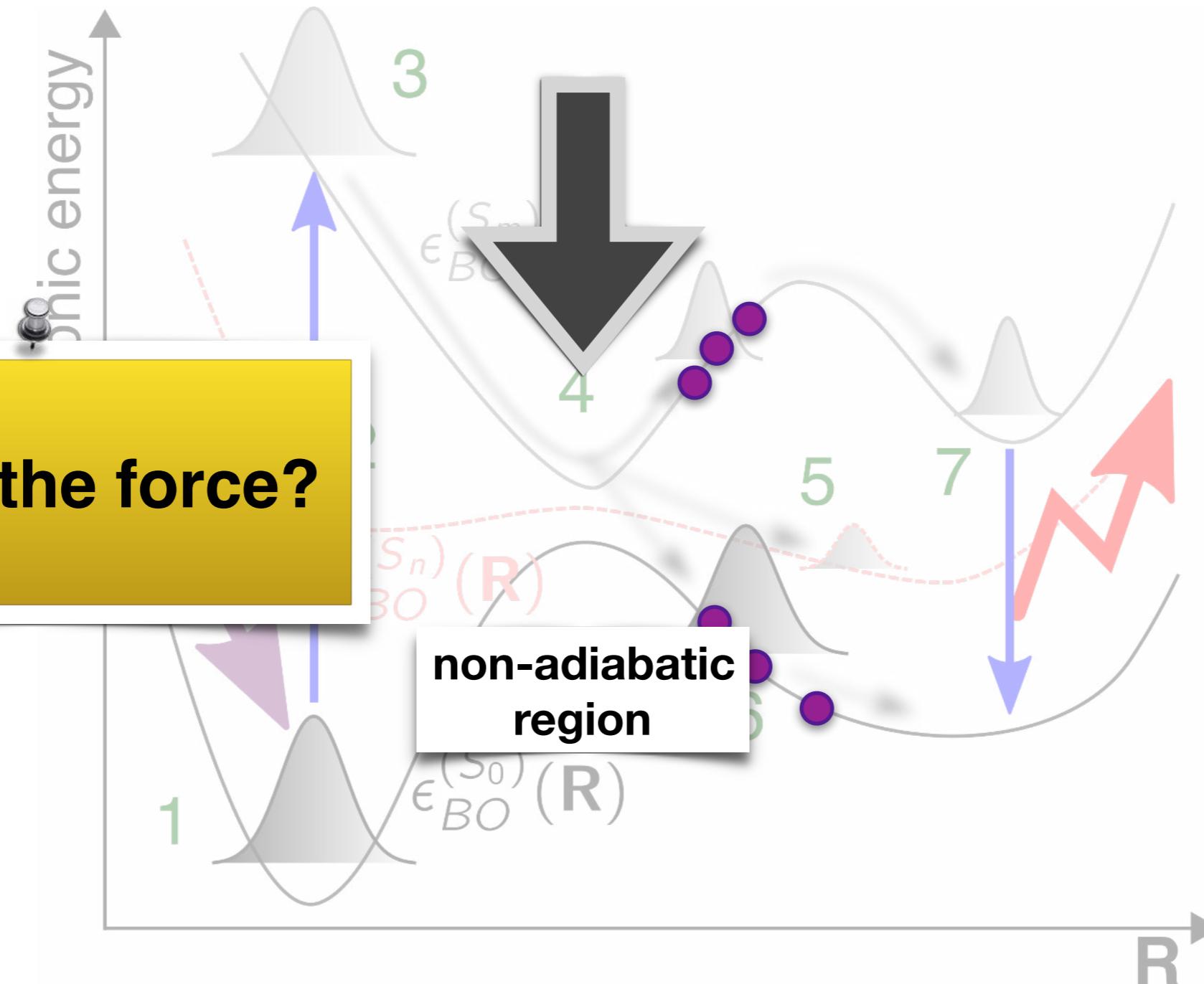
nuclear quantum effects

quantum chemistry

nuclear **classical-like** dynamics

What is the force?

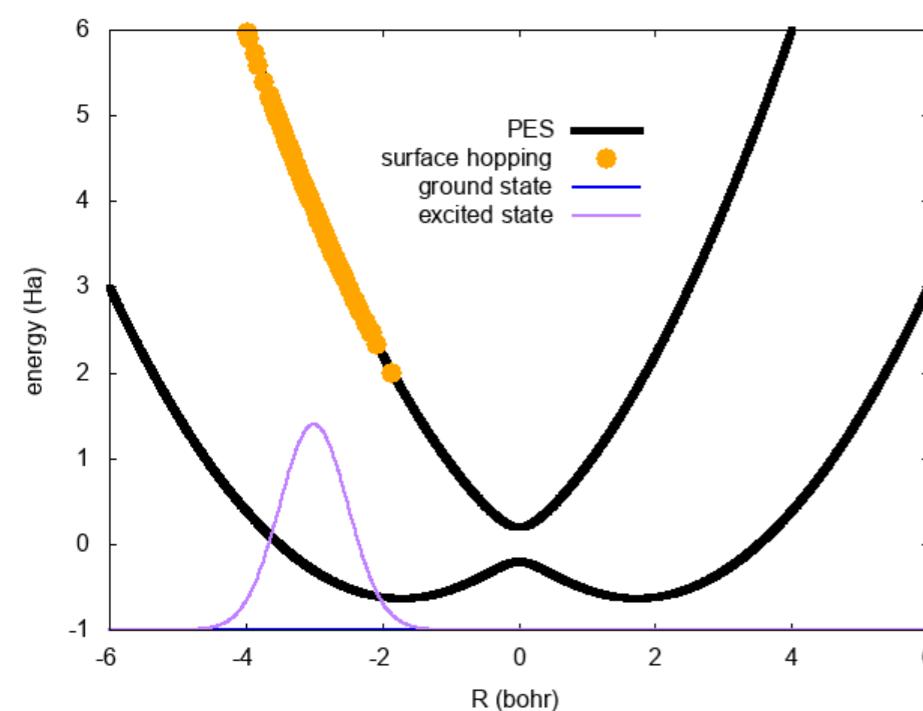
non-adiabatic
region



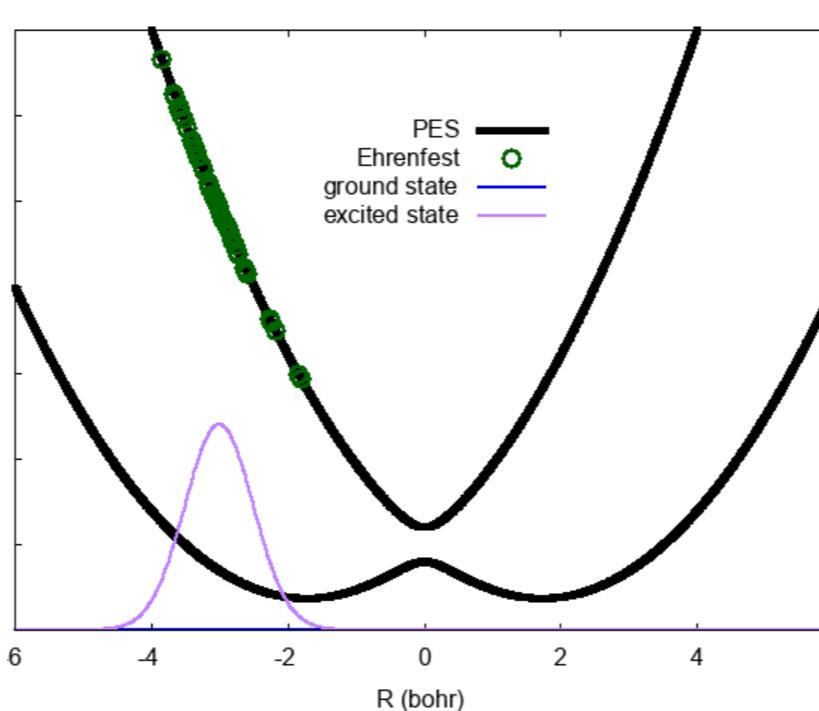
Determining classical-like forces

COMPARISON OF QUANTUM AND CLASSICAL DYNAMICS (model system for photo-excited dynamics)

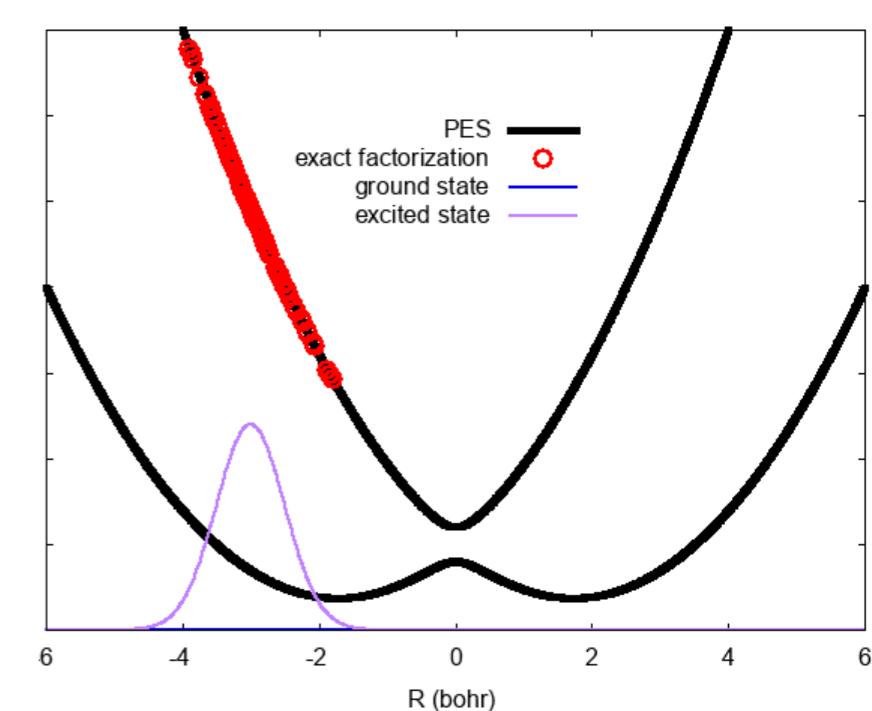
surface hopping



Ehrenfest dynamics



exact factorization



trajectories jump
stochastically

J. C. Tully, *J. Chem. Phys.* **93**
(1990) 1061.

trajectories follow
an average potential

J. C. Tully, *Farad. Discuss.* **110**
(1998) 407.

trajectories evolve
with the exact force



Exact factorization of the electron-nuclear wavefunction

$$P^{(J)}(x, y) = P_y^{(C)}(x) P^{(M)}(y)$$

axiom of probability theory

$$|\Psi(\mathbf{r}, \mathbf{R})|^2 = |\Phi_{\mathbf{R}}(\mathbf{r})|^2 |\chi(\mathbf{R})|^2$$

probabilistic interpretation of the squared modulus of the wavefunction

$$\Psi(\mathbf{r}, \mathbf{R}) = \Phi_{\mathbf{R}}(\mathbf{r})\chi(\mathbf{R})$$

Hunter, *Int. J. Quantum Chem.* **9** (1975)

$$\Psi(\mathbf{r}, \mathbf{R}, t) = \Phi_{\mathbf{R}}(\mathbf{r}, t)\chi(\mathbf{R}, t)$$

Abedi, Maitra, Gross,
Phys. Rev. Lett. **105** (2010)

$$i\hbar\partial_t \Phi_{\mathbf{R}}(\mathbf{r}, t)\chi(\mathbf{R}, t) = [\hat{T}_n + \hat{H}_{el}] \Phi_{\mathbf{R}}(\mathbf{r}, t)\chi(\mathbf{R}, t)$$

electronic equation

nuclear equation

Exact factorization of the electron-nuclear wavefunction

quantum-mechanical
solution based on
quantum chemistry

$$i\hbar\partial_t \Phi_{\mathbf{R}}(\mathbf{r}, t) = \left[\hat{H}_{el} + \hat{U}_{en}[\Phi_{\mathbf{R}}, \chi, \nabla\chi] - \epsilon(\mathbf{R}, t) \right] \Phi_{\mathbf{R}}(\mathbf{r}, t)$$

$$i\hbar\partial_t \chi(\mathbf{R}, t) = \left[\sum_{\nu=1}^{N_n} \frac{[-i\hbar\nabla_{\nu} + \mathbf{A}_{\nu}(\mathbf{R}, t)]^2}{2M_{\nu}} + \epsilon(\mathbf{R}, t) \right] \chi(\mathbf{R}, t)$$

classical solution
based on
trajectories

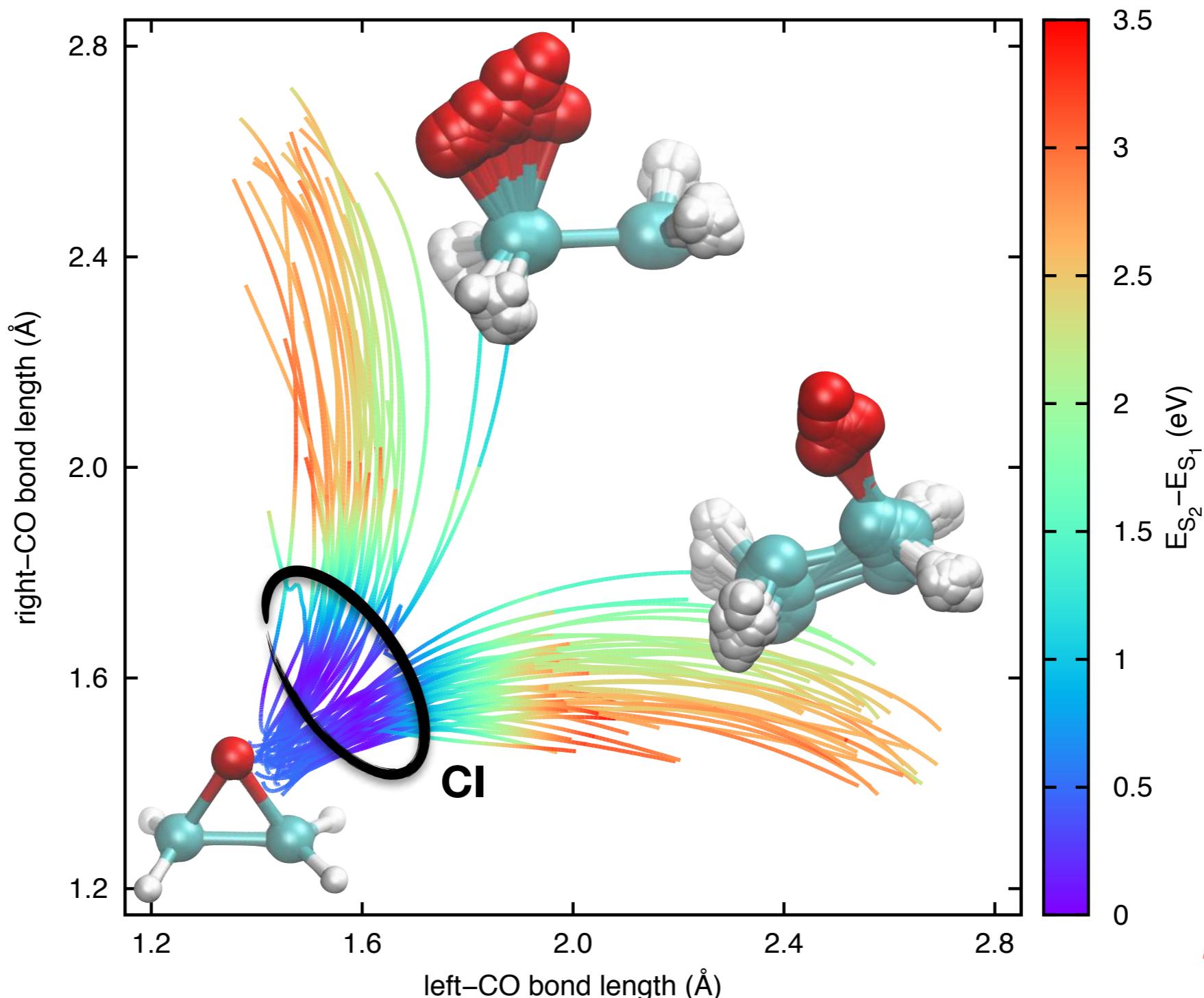
nuclear time-dependent
Schrödinger equation

explicit coupling to the nuclear equation

time-dependent potentials

Photo-induced ring-opening in Oxirane

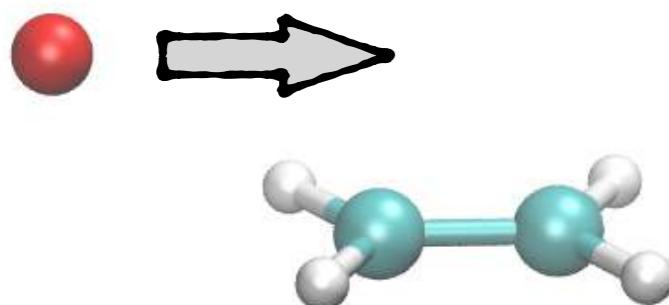
internal conversion = non-radiative relaxation



CPMD

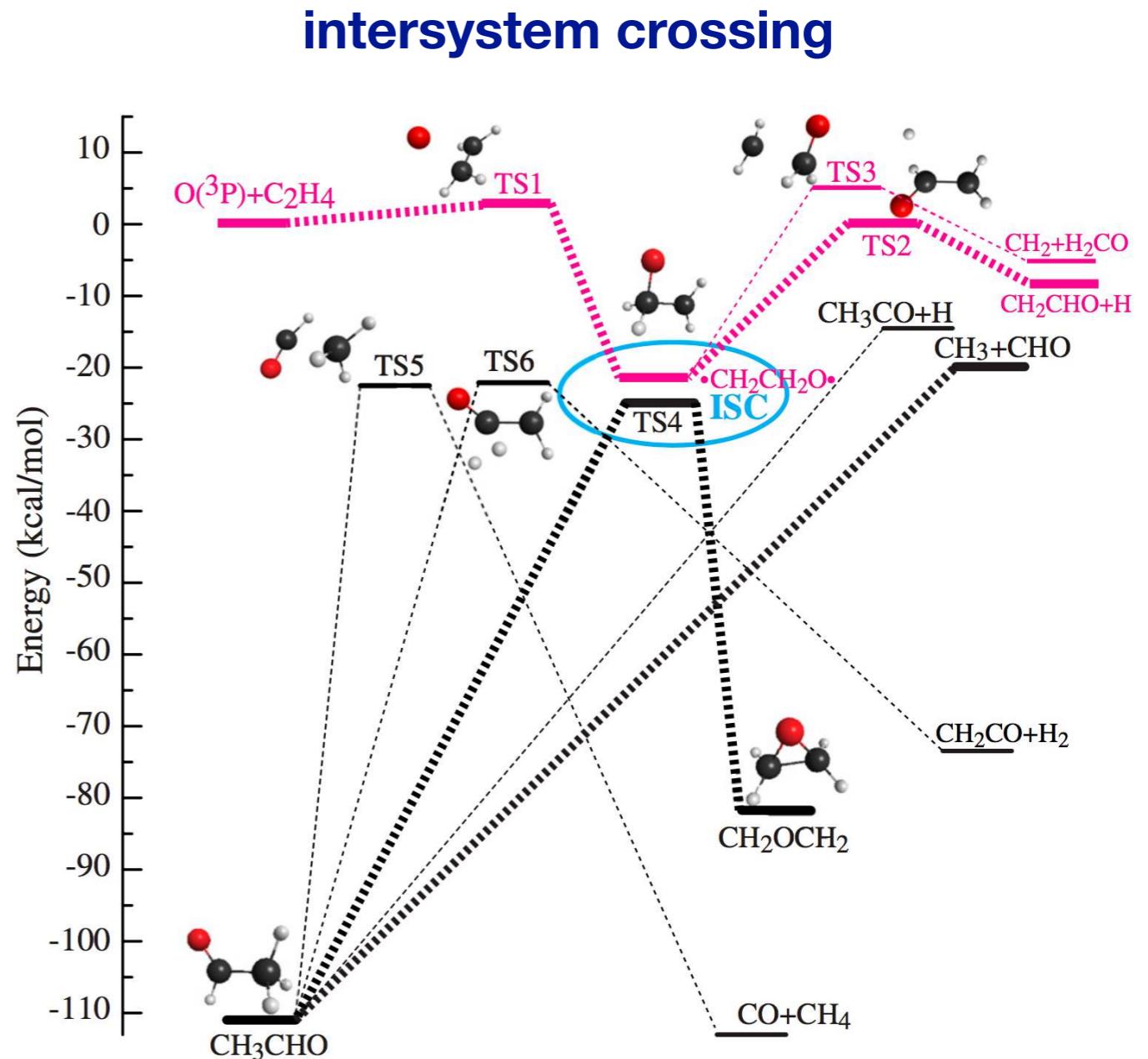
Spin-orbit interactions in ultrafast phenomena

$$i\hbar\partial_t\Psi(\mathbf{x}, \mathbf{R}, t) = [\hat{T}_n + \hat{H}_{el} + \hat{H}_{SO}] \Psi(\mathbf{x}, \mathbf{R}, t)$$



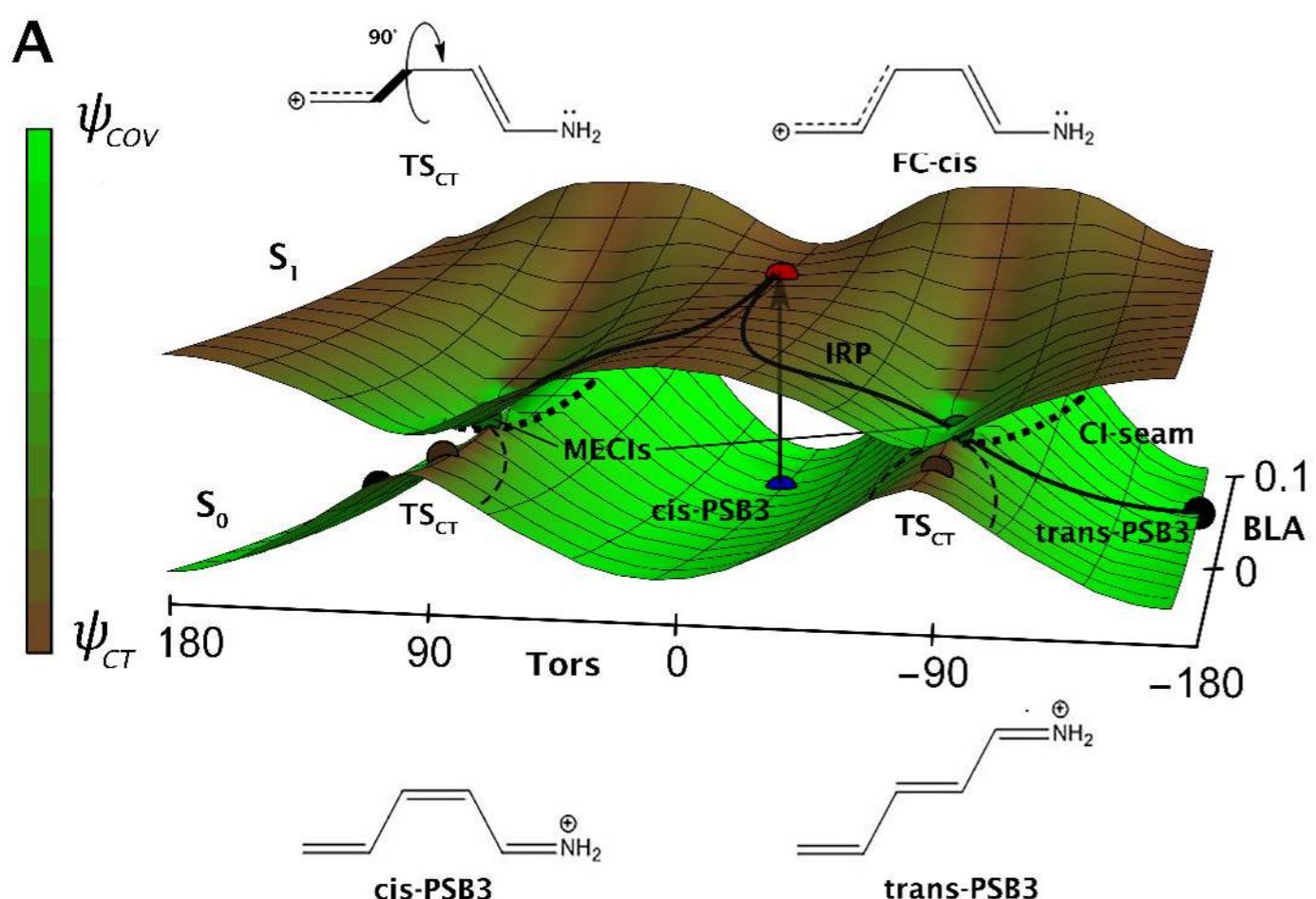
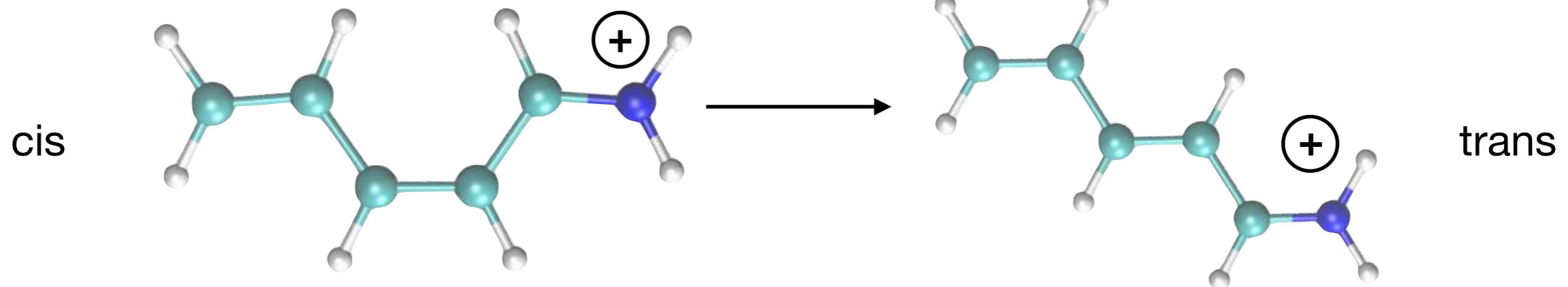
collision dynamics

$O(^3P) + C_2H_4$
including couplings
between
states of different spin
multiplicity, e.g., singlets
and triplets



B. Fu, et al., Proc. Nat. Ac. Sci. 109 (2012) 9733.

Photo-isomerization of a retinal model



E. Marsili, et al., *J. Phys. Chem. A* **123** (2019) 1710.

